

Package: mev (via r-universe)

September 16, 2024

Type Package

Title Modelling of Extreme Values

Version 1.17

Description Various tools for the analysis of univariate, multivariate and functional extremes. Exact simulation from max-stable processes [Dombry, Engelke and Oesting (2016) <[doi:10.1093/biomet/asw008](https://doi.org/10.1093/biomet/asw008)>, R-Pareto processes for various parametric models, including Brown-Resnick (Wadsworth and Tawn, 2014, <[doi:10.1093/biomet/ast042](https://doi.org/10.1093/biomet/ast042)>) and Extremal Student (Thibaud and Opitz, 2015, <[doi:10.1093/biomet/asv045](https://doi.org/10.1093/biomet/asv045)>). Threshold selection methods, including Wadsworth (2016) <[doi:10.1080/00401706.2014.998345](https://doi.org/10.1080/00401706.2014.998345)>, and Northrop and Coleman (2014) <[doi:10.1007/s10687-014-0183-z](https://doi.org/10.1007/s10687-014-0183-z)>. Multivariate extreme diagnostics. Estimation and likelihoods for univariate extremes, e.g., Coles (2001) <[doi:10.1007/978-1-4471-3675-0](https://doi.org/10.1007/978-1-4471-3675-0)>.

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URL <https://lbelzile.github.io/mev/>, <https://github.com/lbelzile/mev/>

BugReports <https://github.com/lbelzile/mev/issues/>

Depends R (>= 3.4)

Imports alabama, methods, nleqslv, Rcpp (>= 0.12.16), Rsolnp, stats,

Suggests boot, cobs, evd, knitr, MASS, mvPot (>= 0.1.4), mvtnorm, gmm, revdbayes, rmarkdown, ismev, tinytest, TruncatedNormal (>= 1.1)

LinkingTo Rcpp, RcppArmadillo

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RoxygenNote 7.3.2

VignetteBuilder knitr

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ByteCompile true

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 abisko

Abisko rainfall

Description

Daily non-zero rainfall measurements in Abisko (Sweden) from January 1913 until December 2014.

Arguments

date	Date of the measurement
precip	rainfall amount (in mm)

Format

a data frame with 15132 rows and two variables

Source

Abisko Scientific Research Station

References

A. Kiriliouk, H. Rootzen, J. Segers and J.L. Wadsworth (2019), *Peaks over thresholds modeling with multivariate generalized Pareto distributions*, *Technometrics*, **61**(1), 123–135, <doi:10.1080/00401706.2018.1462738>

 angextrapo

Bivariate angular dependence function for extrapolation based on rays

Description

The scale parameter $g(w)$ in the Ledford and Tawn approach is estimated empirically for x large as

$$\frac{\Pr(X_P > xw, Y_P > x(1-w))}{\Pr(X_P > x, Y_P > x)}$$

where the sample (X_P, Y_P) are observations on a common unit Pareto scale. The coefficient η is estimated using maximum likelihood as the shape parameter of a generalized Pareto distribution on $\min(X_P, Y_P)$.

Usage

```
angextrapo(dat, qu = 0.95, w = seq(0.05, 0.95, length = 20))
```

Arguments

dat an n by 2 matrix of multivariate observations
 qu quantile level on uniform scale at which to threshold data. Default to 0.95
 w vector of unique angles between 0 and 1 at which to evaluate scale empirically.

Value

a list with elements

- w: angles between zero and one
- g: scale function at a given value of w
- eta: Ledford and Tawn tail dependence coefficient

References

Ledford, A.W. and J. A. Tawn (1996), Statistics for near independence in multivariate extreme values. *Biometrika*, **83**(1), 169–187.

Examples

```
angextrapo(rmev(n = 1000, model = 'log', d = 2, param = 0.5))
```

angmeas	<i>Rank-based transformation to angular measure</i>
---------	---

Description

The method uses the pseudo-polar transformation for suitable norms, transforming the data to pseudo-observations, than marginally to unit Frechet or unit Pareto. Empirical or Euclidean weights are computed and returned alongside with the angular and radial sample for values above threshold(s) th , specified in terms of quantiles of the radial component R or marginal quantiles. Only complete tuples are kept.

Usage

```
angmeas(  
  x,  
  th,  
  Rnorm = c("l1", "l2", "linf"),  
  Anorm = c("l1", "l2", "linf", "arctan"),  
  marg = c("Frechet", "Pareto"),  
  wgt = c("Empirical", "Euclidean"),  
  region = c("sum", "min", "max"),  
  is.angle = FALSE  
)
```

Arguments

x	an n by d sample matrix
th	threshold of length 1 for 'sum', or d marginal thresholds otherwise.
Rnorm	character string indicating the norm for the radial component.
Anorm	character string indicating the norm for the angular component. arctan is only implemented for $d = 2$
marg	character string indicating choice of marginal transformation, either to Frechet or Pareto scale
wgt	character string indicating weighting function for the equation. Can be based on Euclidean or empirical likelihood for the mean
region	character string specifying which observations to consider (and weight). 'sum' corresponds to a radial threshold $\sum x_i > th$, 'min' to $\min x_i > th$ and 'max' to $\max x_i > th$.
is.angle	logical indicating whether observations are already angle with respect to region. Default to FALSE.

Details

The empirical likelihood weighted mean problem is implemented for all thresholds, while the Euclidean likelihood is only supported for diagonal thresholds specified via region=sum.

Value

a list with arguments ang for the $d - 1$ pseudo-angular sample, rad with the radial component and possibly wts if Rnorm='l1' and the empirical likelihood algorithm converged. The Euclidean algorithm always returns weights even if some of these are negative.

a list with components

- ang matrix of pseudo-angular observations
- rad vector of radial contributions
- wts empirical or Euclidean likelihood weights for angular observations

Author(s)

Leo Belzile

References

Einmahl, J.H.J. and J. Segers (2009). Maximum empirical likelihood estimation of the spectral measure of an extreme-value distribution, *Annals of Statistics*, **37**(5B), 2953–2989.

de Carvalho, M. and B. Oumow and J. Segers and M. Warchol (2013). A Euclidean likelihood estimator for bivariate tail dependence, *Comm. Statist. Theory Methods*, **42**(7), 1176–1192.

Owen, A.B. (2001). *Empirical Likelihood*, CRC Press, 304p.

Examples

```
x <- rmev(n=25, d=3, param=0.5, model='log')
wts <- angmeas(x=x, th=0, Rnorm='l1', Anorm='l1', marg='Frechet', wgt='Empirical')
wts2 <- angmeas(x=x, Rnorm='l2', Anorm='l2', marg='Pareto', th=0)
```

angmeasdir

*Dirichlet mixture smoothing of the angular measure***Description**

This function computes the empirical or Euclidean likelihood estimates of the spectral measure and uses the points returned from a call to angmeas to compute the Dirichlet mixture smoothing of de Carvalho, Warchol and Segers (2012), placing a Dirichlet kernel at each observation.

Usage

```
angmeasdir(
  x,
  th,
  Rnorm = c("l1", "l2", "linf"),
  Anorm = c("l1", "l2", "linf", "arctan"),
  marg = c("Frechet", "Pareto"),
  wgt = c("Empirical", "Euclidean"),
  region = c("sum", "min", "max"),
  is.angle = FALSE
)
```

Arguments

x	an n by d sample matrix
th	threshold of length 1 for 'sum', or d marginal thresholds otherwise.
Rnorm	character string indicating the norm for the radial component.
Anorm	character string indicating the norm for the angular component. arctan is only implemented for $d = 2$
marg	character string indicating choice of marginal transformation, either to Frechet or Pareto scale
wgt	character string indicating weighting function for the equation. Can be based on Euclidean or empirical likelihood for the mean
region	character string specifying which observations to consider (and weight). 'sum' corresponds to a radial threshold $\sum x_i > th$, 'min' to $\min x_i > th$ and 'max' to $\max x_i > th$.
is.angle	logical indicating whether observations are already angle with respect to region. Default to FALSE.

Details

The cross-validation bandwidth is the solution of

$$\max_{\nu} \sum_{i=1}^n \log \left\{ \sum_{k=1, k \neq i}^n p_{k,-i} f(\mathbf{w}_i; \nu \mathbf{w}_k) \right\},$$

where f is the density of the Dirichlet distribution, $p_{k,-i}$ is the Euclidean weight obtained from estimating the Euclidean likelihood problem without observation i .

Value

an invisible list with components

- nu bandwidth parameter obtained by cross-validation;
- dirparmat n by d matrix of Dirichlet parameters for the mixtures;
- wts mixture weights.

Examples

```
set.seed(123)
x <- rmev(n=100, d=2, param=0.5, model='log')
out <- angmeasdir(x=x, th=0, Rnorm='l1', Anorm='l1', marg='Frechet', wgt='Empirical')
```

automrl

Automated mean residual life plots

Description

This function implements the automated proposal from Section 2.2 of Langousis et al. (2016) for mean residual life plots. It returns the threshold that minimize the weighted mean square error and moment estimators for the scale and shape parameter based on weighted least squares.

Usage

```
automrl(xdat, kmax, thresh, plot = TRUE, ...)
```

Arguments

xdat	[numeric] vector of observations
kmax	[integer] maximum number of order statistics
thresh	[numeric] vector of thresholds; if missing, uses all order statistics from the 20th largest until kmax as candidates
plot	[logical] if TRUE (default), return a plot of the mean residual life plot with the fitted slope and the chosen threshold
...	additional arguments, currently ignored

Details

The procedure consists in estimating the usual

Value

a list containing

- thresh: selected threshold
- scale: scale parameter estimate
- shape: shape parameter estimate

References

Langousis, A., A. Mamalakis, M. Puliga and R. Deidda (2016). *Threshold detection for the generalized Pareto distribution: Review of representative methods and application to the NOAA NCDC daily rainfall database*, Water Resources Research, **52**, 2659–2681.

confint.eprof

Confidence intervals for profile likelihood objects

Description

Computes confidence intervals for the parameter ψ for profile likelihood objects. This function uses spline interpolation to derive level confidence intervals

Usage

```
## S3 method for class 'eprof'
confint(
  object,
  parm,
  level = 0.95,
  prob = c((1 - level)/2, 1 - (1 - level)/2),
  print = FALSE,
  method = c("cobs", "smooth.spline"),
  ...
)
```

Arguments

object	an object of class eprof, normally the output of gpd.pll or gev.pll .
parm	a specification of which parameters are to be given confidence intervals, either a vector of numbers or a vector of names. If missing, all parameters are considered.
level	confidence level, with default value of 0.95
prob	percentiles, with default giving symmetric 95% confidence intervals

print should a summary be printed. Default to FALSE.
 method string for the method, either cobs (constrained robust B-spline from eponym
 package) or smooth.spline
 ... additional arguments passed to functions. Providing a logical warn=FALSE turns
 off warning messages when the lower or upper confidence interval for psi are
 extrapolated beyond the provided calculations.

Value

returns a 2 by 3 matrix containing point estimates, lower and upper confidence intervals based on the likelihood root and modified version thereof

cvselect	<i>Threshold selection via coefficient of variation</i>
----------	---

Description

This function computes the empirical coefficient of variation and computes a weighted statistic comparing the squared distance with the theoretical coefficient variation corresponding to a specific shape parameter (estimated from the data using a moment estimator as the value minimizing the test statistic, or using maximum likelihood). The procedure stops if there are no more than 10 exceedances above the highest threshold

Usage

```

cvselect(
  xdat,
  thresh,
  method = c("mle", "wcv", "cv"),
  nsim = 999L,
  nthresh = 10L,
  level = 0.05,
  lazy = FALSE
)

```

Arguments

xdat [vector] vector of observations
 thresh [vector] vector of threshold. If missing, set to p^k for $k = 0$ to $k = \text{nthresh}$
 method [string], either moment estimator for the (weighted) coefficient of variation (wcv
 and cv) or maximum likelihood (mle)
 nsim [integer] number of bootstrap replications
 nthresh [integer] number of thresholds, if thresh is not supplied by the user
 level [numeric] probability level for sequential testing procedure
 lazy [logical] compute the bootstrap p-value until the test stops rejecting at level
 level? Default to FALSE

Value

a list with elements

- thresh: value of threshold returned by the procedure, NA if the hypothesis is rejected at all thresholds
- cthresh: sorted vector of candidate thresholds
- cindex: index of selected threshold among cthresh or NA if none returned
- pval: bootstrap p-values, with NA if lazy and the p-value exceeds level at lower thresholds
- shape: shape parameter estimates
- nexc: number of exceedances of each threshold cthresh
- method: estimation method for the shape parameter

References

del Castillo, J. and M. Padilla (2016). *Modelling extreme values by the residual coefficient of variation*, SORT, 40(2), pp. 303–320.

 distg

Distance matrix with geometric anisotropy

Description

The function computes the distance between locations, with geometric anisotropy. The parametrization assumes there is a scale parameter, say σ , so that scale is the distortion for the second component only. The angle rho must lie in $[-\pi/2, \pi/2]$. The dilation and rotation matrix is

$$\begin{pmatrix} \cos(\rho) & \sin(\rho) \\ -\sigma \sin(\rho) & \sigma \cos(\rho) \end{pmatrix}$$

Usage

```
distg(loc, scale, rho)
```

Arguments

loc a d by 2 matrix of locations giving the coordinates of a site per row.
 scale numeric vector of length 1, greater than 1.
 rho angle for the anisotropy, must be larger than $\pi/2$ in modulus.

Value

a d by d square matrix of pairwise distance

egp

*Extended generalised Pareto families***Description**

This function provides the log-likelihood and quantiles for the three different families presented in Papastathopoulos and Tawn (2013). The latter include an additional parameter, κ . All three families share the same tail index as the generalized Pareto distribution, while allowing for lower thresholds. In the case $\kappa = 1$, the models reduce to the generalised Pareto.

`egp.retlev` gives the return levels for the extended generalised Pareto distributions

Arguments

<code>xdat</code>	vector of observations, greater than the threshold
<code>thresh</code>	threshold value
<code>par</code>	parameter vector (κ, σ, ξ) .
<code>model</code>	a string indicating which extended family to fit
<code>show</code>	logical; if TRUE, print the results of the optimization
<code>p</code>	extreme event probability; <code>p</code> must be greater than the rate of exceedance for the calculation to make sense. See Details .
<code>plot</code>	boolean indicating whether or not to plot the return levels

Details

For return levels, the `p` argument can be related to T year exceedances as follows: if there are n_y observations per year, then take `p` to equal $1/(Tn_y)$ to obtain the T -years return level.

Value

`egp.ll` returns the log-likelihood value.

`egp.retlev` returns a plot of the return levels if `plot=TRUE` and a matrix of return levels.

Usage

```
egp.ll(xdat, thresh, par, model=c('egp1', 'egp2', 'egp3'))
```

```
egp.retlev(xdat, thresh, par, model=c('egp1', 'egp2', 'egp3'), p, plot=TRUE)
```

Author(s)

Leo Belzile

References

Papastathopoulos, I. and J. Tawn (2013). Extended generalised Pareto models for tail estimation, *Journal of Statistical Planning and Inference* **143**(3), 131–143.

Examples

```

set.seed(123)
xdat <- mev::rgp(1000, loc = 0, scale = 2, shape = 0.5)
par <- fit.egp(xdat, thresh = 0, model = 'egp3')$par
p <- c(1/1000, 1/1500, 1/2000)
#With multiple thresholds
th <- c(0, 0.1, 0.2, 1)
opt <- tstab.egp(xdat, th, model = 'egp1')
egp.retlev(xdat, opt$thresh, opt$par, 'egp1', p = p)
opt <- tstab.egp(xdat, th, model = 'egp2', plots = NA)
egp.retlev(xdat, opt$thresh, opt$par, 'egp2', p = p)
opt <- tstab.egp(xdat, th, model = 'egp3', plots = NA)
egp.retlev(xdat, opt$thresh, opt$par, 'egp3', p = p)

```

emplik

Self-concordant empirical likelihood for a vector mean

Description

Self-concordant empirical likelihood for a vector mean

Usage

```

emplik(
  dat,
  mu = rep(0, ncol(dat)),
  lam = rep(0, ncol(dat)),
  eps = 1/nrow(dat),
  M = 1e+30,
  thresh = 1e-30,
  itermax = 100
)

```

Arguments

dat	n by d matrix of d-variate observations
mu	d vector of hypothesized mean of dat
lam	starting values for Lagrange multiplier vector, default to zero vector
eps	lower cutoff for $-\log$, with default $1/nrow(dat)$
M	upper cutoff for $-\log$.
thresh	convergence threshold for log likelihood (default of $1e-30$ is aggressive)
itermax	upper bound on number of Newton steps.

Value

a list with components

- logelr log empirical likelihood ratio.
- lam Lagrange multiplier (vector of length d).
- wts n vector of observation weights (probabilities).
- conv boolean indicating convergence.
- niter number of iteration until convergence.
- ndec Newton decrement.
- gradnorm norm of gradient of log empirical likelihood.

Author(s)

Art Owen, C++ port by Leo Belzile

References

Owen, A.B. (2013). Self-concordance for empirical likelihood, *Canadian Journal of Statistics*, **41**(3), 387–397.

eskrain

Eskdalemuir Observatory Daily Rainfall

Description

This dataset contains exceedances of 30mm for daily cumulated rainfall observations over the period 1970-1986. These data were aggregated from hourly series.

Format

a vector with 93 daily cumulated rainfall measurements exceeding 30mm.

Details

The station is one of the rainiest of the whole UK, with an average 1554mm of cumulated rainfall per year. The data consisted of 6209 daily observations, of which 4409 were non-zero. Only the 93 largest observations are provided.

Source

Met Office.

 expme

Exponent measure for multivariate generalized Pareto distributions

Description

Integrated intensity over the region defined by $[0, z]^c$ for logistic, Huesler-Reiss, Brown-Resnick and extremal Student processes.

Usage

```
expme(
  z,
  par,
  model = c("log", "neglog", "hr", "br", "xstud"),
  method = c("TruncatedNormal", "mvtnorm", "mvPot")
)
```

Arguments

z	vector at which to estimate exponent measure
par	list of parameters
model	string indicating the model family
method	string indicating the package from which to extract the numerical integration routine

Value

numeric giving the measure of the complement of $[0, z]$.

Note

The list `par` must contain different arguments depending on the model. For the Brown–Resnick model, the user must supply the conditionally negative definite matrix `Lambda` following the parametrization in Engelke *et al.* (2015) or the covariance matrix `Sigma`, following Wadsworth and Tawn (2014). For the Husler–Reiss model, the user provides the mean and covariance matrix, `m` and `Sigma`. For the extremal student, the covariance matrix `Sigma` and the degrees of freedom `df`. For the logistic model, the strictly positive dependence parameter `alpha`.

Examples

```
## Not run:
# Extremal Student
Sigma <- stats::rWishart(n = 1, df = 20, Sigma = diag(10))[, , 1]
expme(z = rep(1, ncol(Sigma)), par = list(Sigma = cov2cor(Sigma), df = 3), model = "xstud")
# Brown-Resnick model
D <- 5L
loc <- cbind(runif(D), runif(D))
```

```

di <- as.matrix(dist(rbind(c(0, ncol(loc)), loc)))
semivario <- function(d, alpha = 1.5, lambda = 1) {
  (d / lambda)^alpha
}
Vmat <- semivario(di)
Lambda <- Vmat[-1, -1] / 2
expme(z = rep(1, ncol(Lambda)), par = list(Lambda = Lambda), model = "br", method = "mvPot")
Sigma <- outer(Vmat[-1, 1], Vmat[1, -1], "+") - Vmat[-1, -1]
expme(z = rep(1, ncol(Lambda)), par = list(Lambda = Lambda), model = "br", method = "mvPot")

## End(Not run)

```

ext.index	<i>Extremal index estimators based on interexceedance time and gap of exceedances</i>
-----------	---

Description

The function implements the maximum likelihood estimator and iteratively reweighted least square estimators of Suveges (2007) as well as the intervals estimator. The implementation differs from the presentation of the paper in that an iteration limit is enforced to make sure the iterative procedure terminates. Multiple thresholds can be supplied.

Usage

```

ext.index(
  xdat,
  q = 0.95,
  method = c("wls", "mle", "intervals"),
  plot = FALSE,
  warn = FALSE
)

```

Arguments

xdat	numeric vector of observations
q	a vector of quantile levels in (0,1). Defaults to 0.95
method	a string specifying the chosen method. Must be either wls for weighted least squares, mle for maximum likelihood estimation or intervals for the intervals estimator of Ferro and Segers (2003). Partial match is allowed.
plot	logical; if TRUE, plot the extremal index as a function of q
warn	logical; if TRUE, receive a warning when the sample size is too small

Details

The iteratively reweighted least square is a procedure based on the gaps of exceedances $S_n = T_n - 1$. The model is first fitted to non-zero gaps, which are rescaled to have unit exponential scale. The slope between the theoretical quantiles and the normalized gap of exceedances is $b = 1/\theta$, with intercept $a = \log(\theta)/\theta$. As such, the estimate of the extremal index is based on $\hat{\theta} = \exp(\hat{a}/\hat{b})$. The weights are chosen in such a way as to reduce the influence of the smallest values. The estimator exploits the dual role of θ as the parameter of the mean for the interexceedance time as well as the mixture proportion for the non-zero component.

The maximum likelihood is based on an independence likelihood for the rescaled gap of exceedances, namely $\bar{F}(u_n)S(u_n)$. The score equation is equivalent to a quadratic equation in θ and the maximum likelihood estimate is available in closed form. Its validity requires however condition $D^{(2)}(u_n)$ to apply; this should be checked by the user beforehand.

A warning is emitted if the effective sample size is less than 50 observations.

Value

a vector or matrix of estimated extremal index of dimension `length(method)` by `length(q)`.

Author(s)

Leo Belzile

References

Ferro and Segers (2003). Inference for clusters of extreme values, *JRSS: Series B*, **65**(2), 545-556.

Suveges (2007) Likelihood estimation of the extremal index. *Extremes*, **10**(1), 41-55.

Suveges and Davison (2010), Model misspecification in peaks over threshold analysis. *Annals of Applied Statistics*, **4**(1), 203-221.

Fukutome, Liniger and Suveges (2015), Automatic threshold and run parameter selection: a climatology for extreme hourly precipitation in Switzerland. *Theoretical and Applied Climatology*, **120**(3), 403-416.

Examples

```
set.seed(234)
#Moving maxima model with theta=0.5
a <- 1; theta <- 1/(1+a)
sim <- rgev(10001, loc=1/(1+a), scale=1/(1+a), shape=1)
x <- pmax(sim[-length(sim)]*a, sim[-1])
q <- seq(0.9, 0.99, by=0.01)
ext.index(xdat=x, q=q, method=c('wls', 'mle'))
```

 extcoef

Estimators of the extremal coefficient

Description

These functions estimate the extremal coefficient using an approximate sample from the Frechet distribution.

Usage

```
extcoef(
  dat,
  coord = NULL,
  thresh = NULL,
  estimator = c("schlather", "smith", "fmado"),
  standardize = TRUE,
  method = c("nonparametric", "parametric"),
  prob = 0,
  plot = TRUE,
  ...
)
```

Arguments

dat	an n by D matrix of unit Frechet observations
coord	an optional d by D matrix of location coordinates
thresh	threshold parameter (default is to keep all data if prob = 0).
estimator	string indicating which model estimates to compute, one of smith, schlather or fmado.
standardize	logical; should observations be transformed to unit Frechet scale? Default is to transform
method	string indicating which method to use to transform the margins. See Details
prob	probability of not exceeding threshold thresh
plot	logical; should cloud of pairwise empirical estimates be plotted? Default to TRUE.
...	additional parameters passed to the function, currently ignored.

Details

The **Smith** estimator: suppose $Z(x)$ is simple max-stable vector (i.e., with unit Frechet marginals). Then $1/Z$ is unit exponential and $1/\max(Z(s_1), Z(s_2))$ is exponential with rate $\theta = \max\{Z(s_1), Z(s_2)\}$. The extremal index for the pair can therefore be calculated using the reciprocal mean.

The **Schlather and Tawn** estimator: the likelihood of the naive estimator for a pair of two sites A is

$$\text{card} \left\{ j : \max_{i \in A} X_i^{(j)} \bar{X}_i > z \right\} \log(\theta_A) - \theta_A \sum_{j=1}^n \left[\max \left\{ z, \max_{i \in A} (X_i^{(j)} \bar{X}_i) \right\} \right]^{-1},$$

where $\bar{X}_i = n^{-1} \sum_{j=1}^n 1/X_i^{(j)}$ is the harmonic mean and z is a threshold on the unit Frechet scale. The search for the maximum likelihood estimate for every pair A is restricted to the interval $[1, 3]$. A binned version of the extremal coefficient cloud is also returned. The Schlather estimator is not self-consistent. The Schlather and Tawn estimator includes as special case the Smith estimator if we do not censor the data ($p = 0$) and do not standardize observations by their harmonic mean.

The **F-madogram** estimator is a non-parametric estimate based on a stationary process Z ; the extremal coefficient satisfies

$$\theta(h) = \frac{1 + 2\nu(h)}{1 - 2\nu(h)},$$

where

$$\nu(h) = \frac{1}{2} \mathbb{E}[|F(Z(s+h)) - F(Z(s))|]$$

The implementation only uses complete pairs to calculate the relative ranks.

All estimators are coded in plain R and computations are not optimized. The estimation time can therefore be significant for large data sets. If there are no missing observations, the routine `fmadogram` from the `SpatialExtremes` package should be preferred as it is noticeably faster.

The data will typically consist of max-stable vectors or block maxima. Both of the Smith and the Schlather–Tawn estimators require unit Frechet margins; the margins will be standardized to the unit Frechet scale, either parametrically or nonparametrically unless `standardize = FALSE`. If `method = "parametric"`, a parametric GEV model is fitted to each column of `dat` using maximum likelihood estimation and transformed back using the probability integral transform. If `method = "nonparametric"`, using the empirical distribution function. The latter is the default, as it is appreciably faster.

Value

an invisible list with vectors `dist` if `coord` is non-null or else a matrix of pairwise indices `ind`, `extcoef` and the supplied estimator, `fmado` and `binned`. If `estimator == "schlather"`, an additional matrix with 2 columns containing the binned distance `binned` with the `h` and the binned extremal coefficient.

References

- Schlather, M. and J. Tawn (2003). A dependence measure for multivariate and spatial extremes, *Biometrika*, **90**(1), pp.139–156.
- Cooley, D., P. Naveau and P. Poncet (2006). Variograms for spatial max-stable random fields, In: Bertail P., Soulier P., Doukhan P. (eds) *Dependence in Probability and Statistics*. Lecture Notes in Statistics, vol. 187. Springer, New York, NY
- R. J. Erhardt, R. L. Smith (2012), Approximate Bayesian computing for spatial extremes, *Computational Statistics and Data Analysis*, **56**, pp.1468–1481.

Examples

```
## Not run:
coord <- 10*cbind(runif(50), runif(50))
di <- as.matrix(dist(coord))
dat <- rmev(n = 1000, d = 100, param = 3, sigma = exp(-di/2), model = 'xstud')
res <- extcoef(dat = dat, coord = coord)
# Extremal Student extremal coefficient function

XT.extcoeffun <- function(h, nu, corrfun, ...){
  if(!is.function(corrfun)){
    stop('Invalid function \'corrfun\'.')
  }
  h <- unique(as.vector(h))
  rhoh <- sapply(h, corrfun, ...)
  cbind(h = h, extcoef = 2*pt(sqrt((nu+1)*(1-rhoh)/(1+rhoh)), nu+1))
}
#This time, only one graph with theoretical extremal coef
plot(res$dist, res$extcoef, ylim = c(1,2), pch = 20); abline(v = 2, col = 'gray')
extcoefxt <- XT.extcoeffun(seq(0, 10, by = 0.1), nu = 3,
  corrfun = function(x){exp(-x/2)})
lines(extcoefxt[, 'h'], extcoefxt[, 'extcoef'], type = 'l', col = 'blue', lwd = 2)
# Brown--Resnick extremal coefficient function
BR.extcoeffun <- function(h, vario, ...){
  if(!is.function(vario)){
    stop('Invalid function \'vario\'.')
  }
  h <- unique(as.vector(h))
  gammah <- sapply(h, vario, ...)
  cbind(h = h, extcoef = 2*pnorm(sqrt(gammah/4)))
}
extcoefbr <- BR.extcoeffun(seq(0, 20, by = 0.25), vario = function(x){2*x^0.7})
lines(extcoefbr[, 'h'], extcoefbr[, 'extcoef'], type = 'l', col = 'orange', lwd = 2)

coord <- 10*cbind(runif(20), runif(20))
di <- as.matrix(dist(coord))
dat <- rmev(n = 1000, d = 20, param = 3, sigma = exp(-di/2), model = 'xstud')
res <- extcoef(dat = dat, coord = coord, estimator = "smith")

## End(Not run)
```

Description

Density function, distribution function, quantile function and random generation for the extended generalized Pareto distribution (GPD) with scale and shape parameters.

Arguments

q	vector of quantiles
x	vector of observations
p	vector of probabilities
n	sample size
prob	mixture probability for model type 4
kappa	shape parameter for type 1, 3 and 4
delta	additional parameter for type 2, 3 and 4
sigma	scale parameter
xi	shape parameter
type	integer between 0 to 5 giving the model choice
step	function of step size for discretization with default 0, corresponding to continuous quantiles
log	logical; should the log-density be returned (default to FALSE)?
unifsamp	sample of uniform; if provided, the data will be used in place of new uniform random variates
censoring	numeric vector of length 2 containing the lower and upper bound for censoring

Details

The extended generalized Pareto families proposed in Naveau *et al.* (2016) retain the tail index of the distribution while being compliant with the theoretical behavior of extreme low rainfall. There are five proposals, the first one being equivalent to the GP distribution.

- type 0 corresponds to uniform carrier, $G(u) = u$.
- type 1 corresponds to a three parameters family, with carrier $G(u) = u^\kappa$.
- type 2 corresponds to a three parameters family, with carrier $G(u) = 1 - V_\delta((1 - u)^\delta)$.
- type 3 corresponds to a four parameters family, with carrier

$$G(u) = 1 - V_\delta((1 - u)^\delta))^{\kappa/2}$$

- type 4 corresponds to a five parameter model (a mixture of type 2, with $G(u) = pu^\kappa + (1 - p) * u^\delta$

Usage

```
pextgp(q, prob=NA, kappa=NA, delta=NA, sigma=NA, xi=NA, type=1)
dextgp(x, prob=NA, kappa=NA, delta=NA, sigma=NA, xi=NA, type=1, log=FALSE)
qextgp(p, prob=NA, kappa=NA, delta=NA, sigma=NA, xi=NA, type=1)
rextgp(n, prob=NA, kappa=NA, delta=NA, sigma=NA, xi=NA, type=1, unifsamp=NULL, censoring=c(0,Inf))
```

Author(s)

Raphael Huser and Philippe Naveau

References

Naveau, P., R. Huser, P. Ribereau, and A. Hannart (2016), Modeling jointly low, moderate, and heavy rainfall intensities without a threshold selection, *Water Resour. Res.*, 52, 2753-2769, doi : 10.1002/2015WR018552.

extgp.G

Carrier distribution for the extended GP distributions of Naveau et al.

Description

Density, distribution function, quantile function and random number generation for the carrier distributions of the extended Generalized Pareto distributions.

Arguments

u	vector of observations (dextgp.G), probabilities (qextgp.G) or quantiles (pextgp.G), in [0, 1]
prob	mixture probability for model type 4
kappa	shape parameter for type 1, 3 and 4
delta	additional parameter for type 2, 3 and 4
type	integer between 0 to 5 giving the model choice
log	logical; should the log-density be returned (default to FALSE)?
n	sample size
unifsamp	sample of uniform; if provided, the data will be used in place of new uniform random variates
censoring	numeric vector of length 2 containing the lower and upper bound for censoring
direct	logical; which method to use for sampling in model of type 4?

Usage

```
pextgp.G(u, type=1, prob, kappa, delta)
dextgp.G(u, type=1, prob=NA, kappa=NA, delta=NA, log=FALSE)
qextgp.G(u, type=1, prob=NA, kappa=NA, delta=NA)
rextgp.G(n, prob=NA, kappa=NA, delta=NA, type=1, unifsamp=NULL, direct=FALSE, censoring=c(0,1))
```

Author(s)

Raphael Huser and Philippe Naveau

See Also

[extgp](#)

 extremo

Pairwise extremogram for max-risk functional

Description

The function computes the pairwise *chi* estimates and plots them as a function of the distance between sites.

Usage

```
extremo(dat, margp, coord, scale = 1, rho = 0, plot = FALSE, ...)
```

Arguments

dat	data matrix
margp	marginal probability above which to threshold observations
coord	matrix of coordinates (one site per row)
scale	geometric anisotropy scale parameter
rho	geometric anisotropy angle parameter
plot	logical; should a graph of the pairwise estimates against distance? Default to FALSE
...	additional arguments passed to plot

Value

an invisible matrix with pairwise estimates of chi along with distance (unsorted)

Examples

```
## Not run:
lon <- seq(650, 720, length = 10)
lat <- seq(215, 290, length = 10)
# Create a grid
grid <- expand.grid(lon,lat)
coord <- as.matrix(grid)
dianiso <- distg(coord, 1.5, 0.5)
sgrid <- scale(grid, scale = FALSE)
# Specify marginal parameters `loc` and `scale` over grid
eta <- 26 + 0.05*sgrid[,1] - 0.16*sgrid[,2]
tau <- 9 + 0.05*sgrid[,1] - 0.04*sgrid[,2]
# Parameter matrix of Huesler--Reiss
# associated to power variogram
Lambda <- ((dianiso/30)^0.7)/4
# Regular Euclidean distance between sites
di <- distg(coord, 1, 0)
# Simulate generalized max-Pareto field
set.seed(345)
```

```

simul <- rgparp(n = 1000, thresh = 50, shape = 0.1, riskf = "max",
              scale = tau, loc = eta, sigma = Lambda, model = "hr")
extdat <- extremo(dat = simul, margp = 0.98, coord = coord,
                scale = 1.5, rho = 0.5, plot = TRUE)

# Constrained optimization
# Minimize distance between extremal coefficient from fitted variogram
mindistpvario <- function(par, emp, coord){
alpha <- par[1]; if(!isTRUE(all(alpha > 0, alpha < 2))){return(1e10)}
scale <- par[2]; if(scale <= 0){return(1e10)}
a <- par[3]; if(a<1){return(1e10)}
rho <- par[4]; if(abs(rho) >= pi/2){return(1e10)}
semivariomat <- power.vario(distg(coord, a, rho), alpha = alpha, scale = scale)
  sum((2*(1-pnorm(sqrt(semivariomat[lower.tri(semivariomat)]/2))) - emp)^2)
}

hin <- function(par, ...){
  c(1.99-par[1], -1e-5 + par[1],
    -1e-5 + par[2],
    par[3]-1,
    pi/2 - par[4],
    par[4]+pi/2)
}

opt <- alabama::auglag(par = c(0.7, 30, 1, 0),
                    hin = hin,
                    fn = function(par){
                      mindistpvario(par, emp = extdat[, 'prob'], coord = coord)})

stopifnot(opt$kk1, opt$kk2)
# Plotting the extremogram in the deformed space
distfa <- distg(loc = coord, opt$par[3], opt$par[4])
plot(
  x = c(distfa[lower.tri(distfa)]),
  y = extdat[,2],
  pch = 20,
  yaxs = "i",
  xaxs = "i",
  bty = 'l',
  xlab = "distance",
  ylab = "cond. prob. of exceedance",
  ylim = c(0,1))
lines(
  x = (distvec <- seq(0,200, length = 1000)),
  col = 2, lwd = 2,
  y = 2*(1-pnorm(sqrt(power.vario(distvec, alpha = opt$par[1],
                                scale = opt$par[2]/2))))))

## End(Not run)

```


Description

The function `tstab.egp` provides classical threshold stability plot for (κ, σ, ξ) . The fitted parameter values are displayed with pointwise normal 95% confidence intervals. The function returns an invisible list with parameter estimates and standard errors, and p-values for the Wald test that $\kappa = 1$. The plot is for the modified scale (as in the generalised Pareto model) and as such it is possible that the modified scale be negative. `tstab.egp` can also be used to fit the model to multiple thresholds.

Usage

```
fit.egp(xdat, thresh, model = c("egp1", "egp2", "egp3"), init, show = FALSE)
```

```
tstab.egp(
  xdat,
  thresh,
  model = c("egp1", "egp2", "egp3"),
  plots = 1:3,
  umin,
  umax,
  nint,
  changepar = TRUE,
  ...
)
```

Arguments

<code>xdat</code>	vector of observations, greater than the threshold
<code>thresh</code>	threshold value
<code>model</code>	a string indicating which extended family to fit
<code>init</code>	vector of initial values, with $\log(\kappa)$ and $\log(\sigma)$; can be omitted.
<code>show</code>	logical; if TRUE, print the results of the optimization
<code>plots</code>	vector of integers specifying which parameter stability to plot (if any); passing NA results in no plots
<code>umin</code>	optional minimum value considered for threshold (if <code>thresh</code> is not provided)
<code>umax</code>	optional maximum value considered for threshold (if <code>thresh</code> is not provided)
<code>nint</code>	optional integer number specifying the number of thresholds to test.
<code>changepar</code>	logical; if TRUE, the graphical parameters (via a call to <code>par</code>) are modified.
<code>...</code>	additional arguments for the plot function, currently ignored

Details

`fit.egp` is a numerical optimization routine to fit the extended generalised Pareto models of Papathopoulos and Tawn (2013), using maximum likelihood estimation.

Value

`fit.egp` outputs the list returned by `optim`, which contains the parameter values, the hessian and in addition the standard errors

`tstab.egp` returns a plot(s) of the parameters fit over the range of provided thresholds, with point-wise normal confidence intervals; the function also returns an invisible list containing notably the matrix of point estimates (`par`) and standard errors (`se`).

Author(s)

Leo Belzile

References

Papastathopoulos, I. and J. Tawn (2013). Extended generalised Pareto models for tail estimation, *Journal of Statistical Planning and Inference* **143**(3), 131–143.

Examples

```
xdat <- mev::rgp(
  n = 100,
  loc = 0,
  scale = 1,
  shape = 0.5)
fitted <- fit.egp(
  xdat = xdat,
  thresh = 1,
  model = "egp2",
  show = TRUE)
thresh <- mev::qgp(seq(0.1, 0.5, by = 0.05), 0, 1, 0.5)
tstab.egp(
  xdat = xdat,
  thresh = thresh,
  model = "egp2",
  plots = 1:3)
```

fit.extgp

Fit an extended generalized Pareto distribution of Naveau et al.

Description

This is a wrapper function to obtain PWM or MLE estimates for the extended GP models of Naveau et al. (2016) for rainfall intensities. The function calculates confidence intervals by means of nonparametric percentile bootstrap and returns histograms and QQ plots of the fitted distributions. The function handles both censoring and rounding.

Usage

```
fit.extgp(
  data,
  model = 1,
  method = c("mle", "pwm"),
  init,
  censoring = c(0, Inf),
  rounded = 0,
  confint = FALSE,
  R = 1000,
  ncpus = 1,
  plots = TRUE
)
```

Arguments

data	data vector.
model	integer ranging from 0 to 4 indicating the model to select (see extgp).
method	string; either 'mle' for maximum likelihood, or 'pwm' for probability weighted moments, or both.
init	vector of initial values, comprising of p , κ , δ , σ , ξ (in that order) for the optimization. All parameters may not appear depending on model.
censoring	numeric vector of length 2 containing the lower and upper bound for censoring; <code>censoring=c(0, Inf)</code> is equivalent to no censoring.
rounded	numeric giving the instrumental precision (and rounding of the data), with default of 0.
confint	logical; should confidence interval be returned (percentile bootstrap).
R	integer; number of bootstrap replications.
ncpus	integer; number of CPUs for parallel calculations (default: 1).
plots	logical; whether to produce histogram and density plots.

Details

The different models include the following transformations:

- model 0 corresponds to uniform carrier, $G(u) = u$.
- model 1 corresponds to a three parameters family, with carrier $G(u) = u^\kappa$.
- model 2 corresponds to a three parameters family, with carrier $G(u) = 1 - V_\delta((1 - u)^\delta)$.
- model 3 corresponds to a four parameters family, with carrier

$$G(u) = 1 - V_\delta((1 - u)^\delta)^{\kappa/2}$$

- model 4 corresponds to a five parameter model (a mixture of type 2, with $G(u) = pu^\kappa + (1 - p) * u^\delta$

Author(s)

Raphael Huser and Philippe Naveau

References

Naveau, P., R. Huser, P. Ribereau, and A. Hannart (2016), Modeling jointly low, moderate, and heavy rainfall intensities without a threshold selection, *Water Resour. Res.*, 52, 2753-2769, doi:10.1002/2015WR018552.

See Also

[egp.fit](#), [egp](#), [extgp](#)

Examples

```
## Not run:
data(rain, package = "ismev")
fit.extgp(rain[rain>0], model=1, method = 'mle', init = c(0.9, gp.fit(rain, 0)$est),
  rounded = 0.1, confint = TRUE, R = 20)

## End(Not run)
```

fit.gev

Maximum likelihood estimation for the generalized extreme value distribution

Description

This function returns an object of class `mev_gev`, with default methods for printing and quantile-quantile plots. The default starting values are the solution of the probability weighted moments.

Usage

```
fit.gev(
  xdat,
  start = NULL,
  method = c("nlminb", "BFGS"),
  show = FALSE,
  fpar = NULL,
  warnSE = FALSE
)
```

Arguments

<code>xdat</code>	a numeric vector of data to be fitted.
<code>start</code>	named list of starting values
<code>method</code>	string indicating the outer optimization routine for the augmented Lagrangian. One of <code>nlminb</code> or <code>BFGS</code> .

show	logical; if TRUE (the default), print details of the fit.
fpar	a named list with optional fixed components loc, scale and shape
warnSE	logical; if TRUE, a warning is printed if the standard errors cannot be returned from the observed information matrix when the shape is less than -0.5.

Value

a list containing the following components:

- estimate a vector containing the maximum likelihood estimates.
- std.err a vector containing the standard errors.
- vcov the variance covariance matrix, obtained as the numerical inverse of the observed information matrix.
- method the method used to fit the parameter.
- nllh the negative log-likelihood evaluated at the parameter estimate.
- convergence components taken from the list returned by `auglag`. Values other than 0 indicate that the algorithm likely did not converge.
- counts components taken from the list returned by `auglag`.
- xdat vector of data

Examples

```
xdat <- mev::rgev(n = 100)
fit.gev(xdat, show = TRUE)
# Example with fixed parameter
fit.gev(xdat, show = TRUE, fpar = list(shape = 0))
```

fit.gpd

Maximum likelihood estimation for the generalized Pareto distribution

Description

Numerical optimization of the generalized Pareto distribution for data exceeding threshold. This function returns an object of class `mev_gpd`, with default methods for printing and quantile-quantile plots.

Usage

```
fit.gpd(
  xdat,
  threshold = 0,
  method = "Grimshaw",
  show = FALSE,
  MCMC = NULL,
  k = 4,
```

```

    tol = 1e-08,
    fpar = NULL,
    warnSE = FALSE
  )

```

Arguments

xdat	a numeric vector of data to be fitted.
threshold	the chosen threshold.
method	the method to be used. See Details . Can be abbreviated.
show	logical; if TRUE (the default), print details of the fit.
MCMC	NULL for frequentist estimates, otherwise a boolean or a list with parameters passed. If TRUE, runs a Metropolis-Hastings sampler to get posterior mean estimates. Can be used to pass arguments <code>niter</code> , <code>burnin</code> and <code>thin</code> to the sampler as a list.
k	bound on the influence function (method = "obre"); the constant k is a robustness parameter (higher bounds are more efficient, low bounds are more robust). Default to 4, must be larger than $\sqrt{2}$.
tol	numerical tolerance for OBRE weights iterations (method = "obre"). Default to 1e-8.
fpar	a named list with fixed parameters, either scale or shape
warnSE	logical; if TRUE, a warning is printed if the standard errors cannot be returned from the observed information matrix when the shape is less than -0.5.

Details

The default method is 'Grimshaw', which maximizes the profile likelihood for the ratio scale/shape. Other options include 'obre' for optimal B -robust estimator of the parameter of Dupuis (1998), vanilla maximization of the log-likelihood using constrained optimization routine 'auglag', 1-dimensional optimization of the profile likelihood using `nlm` and `optim`. Method 'ismev' performs the two-dimensional optimization routine `gpd.fit` from the `ismev` library, with in addition the algebraic gradient. The approximate Bayesian methods ('zs' and 'zhang') are extracted respectively from Zhang and Stephens (2009) and Zhang (2010) and consists of a approximate posterior mean calculated via importance sampling assuming a GPD prior is placed on the parameter of the profile likelihood.

Value

If method is neither 'zs' nor 'zhang', a list containing the following components:

- `estimate` a vector containing the scale and shape parameters (optimized and fixed).
- `std.err` a vector containing the standard errors. For method = "obre", these are Huber's robust standard errors.
- `vcov` the variance covariance matrix, obtained as the numerical inverse of the observed information matrix. For method = "obre", this is the sandwich Godambe matrix inverse.
- `threshold` the threshold.

- method the method used to fit the parameter. See details.
- nllh the negative log-likelihood evaluated at the parameter estimate.
- nat number of points lying above the threshold.
- pat proportion of points lying above the threshold.
- convergence components taken from the list returned by `optim`. Values other than 0 indicate that the algorithm likely did not converge (in particular 1 and 50).
- counts components taken from the list returned by `optim`.
- exceedances excess over the threshold.

Additionally, if `method = "obre"`, a vector of OBRE weights.

Otherwise, a list containing

- threshold the threshold.
- method the method used to fit the parameter. See **Details**.
- nat number of points lying above the threshold.
- pat proportion of points lying above the threshold.
- approx.mean a vector containing containing the approximate posterior mean estimates.

and in addition if `MCMC` is neither `FALSE`, nor `NULL`

- post.mean a vector containing the posterior mean estimates.
- post.se a vector containing the posterior standard error estimates.
- accept.rate proportion of points lying above the threshold.
- niter length of resulting Markov Chain
- burnin amount of discarded iterations at start, capped at 10000.
- thin thinning integer parameter describing

Note

Some of the internal functions (which are hidden from the user) allow for modelling of the parameters using covariates. This is not currently implemented within `gp.fit`, but users can call internal functions should they wish to use these features.

Author(s)

Scott D. Grimshaw for the Grimshaw option. Paul J. Northrop and Claire L. Coleman for the methods `optim`, `nlm` and `ismev`. J. Zhang and Michael A. Stephens (2009) and Zhang (2010) for the `zs` and `zhang` approximate methods and L. Belzile for methods `auglag` and `obre`, the wrapper and MCMC samplers.

If `show = TRUE`, the optimal B robust estimated weights for the largest observations are printed alongside with the p -value of the latter, obtained from the empirical distribution of the weights. This diagnostic can be used to guide threshold selection: small weights for the r -largest order statistics indicate that the robust fit is driven by the lower tail and that the threshold should perhaps be increased.

References

- Davison, A.C. (1984). Modelling excesses over high thresholds, with an application, in *Statistical extremes and applications*, J. Tiago de Oliveira (editor), D. Reidel Publishing Co., 461–482.
- Grimshaw, S.D. (1993). Computing Maximum Likelihood Estimates for the Generalized Pareto Distribution, *Technometrics*, **35**(2), 185–191.
- Northrop, P.J. and C. L. Coleman (2014). Improved threshold diagnostic plots for extreme value analyses, *Extremes*, **17**(2), 289–303.
- Zhang, J. (2010). Improving on estimation for the generalized Pareto distribution, *Technometrics* **52**(3), 335–339.
- Zhang, J. and M. A. Stephens (2009). A new and efficient estimation method for the generalized Pareto distribution. *Technometrics* **51**(3), 316–325.
- Dupuis, D.J. (1998). Exceedances over High Thresholds: A Guide to Threshold Selection, *Extremes*, **1**(3), 251–261.

See Also

[fpot](#) and [gpd.fit](#)

Examples

```
data(eskrain)
fit.gpd(eskrain, threshold = 35, method = 'Grimshaw', show = TRUE)
fit.gpd(eskrain, threshold = 30, method = 'zs', show = TRUE)
```

fit.pp

Maximum likelihood estimation of the point process of extremes

Description

Data above threshold is modelled using the limiting point process of extremes.

Usage

```
fit.pp(  
  xdat,  
  threshold = 0,  
  npp = 1,  
  np = NULL,  
  method = c("nlminb", "BFGS"),  
  start = NULL,  
  show = FALSE,  
  fpar = NULL,  
  warnSE = FALSE  
)
```


Arguments

xdat	a numeric vector of data to be fitted.
threshold	the chosen threshold.
npp	number of observation per period. See Details
np	number of periods of data, if xdat only contains exceedances.
method	the method to be used. See Details . Can be abbreviated.
start	named list of starting values
show	logical; if TRUE (the default), print details of the fit.
fpar	a named list with optional fixed components loc, scale and shape
warnSE	logical; if TRUE, a warning is printed if the standard errors cannot be returned from the observed information matrix when the shape is less than -0.5.

Details

The parameter npp controls the frequency of observations. If data are recorded on a daily basis, using a value of npp = 365.25 yields location and scale parameters that correspond to those of the generalized extreme value distribution fitted to block maxima.

Value

a list containing the following components:

- estimate a vector containing all parameters (optimized and fixed).
- std.err a vector containing the standard errors.
- vcov the variance covariance matrix, obtained as the numerical inverse of the observed information matrix.
- threshold the threshold.
- method the method used to fit the parameter. See details.
- nllh the negative log-likelihood evaluated at the parameter estimate.
- nat number of points lying above the threshold.
- pat proportion of points lying above the threshold.
- convergence components taken from the list returned by `optim`. Values other than 0 indicate that the algorithm likely did not converge (in particular 1 and 50).
- counts components taken from the list returned by `optim`.

References

Coles, S. (2001), An introduction to statistical modelling of extreme values. Springer : London, 208p.

Examples

```
data(eskrain)
pp_mle <- fit.pp(eskrain, threshold = 30, np = 6201)
plot(pp_mle)
```

fit.rlarg	<i>Maximum likelihood estimates of point process for the r-largest observations</i>
-----------	---

Description

This uses a constrained optimization routine to return the maximum likelihood estimate based on an n by r matrix of observations. Observations should be ordered, i.e., the r -largest should be in the last column.

Usage

```
fit.rlarg(
  xdat,
  start = NULL,
  method = c("nlminb", "BFGS"),
  show = FALSE,
  fpar = NULL,
  warnSE = FALSE
)
```

Arguments

xdat	a numeric vector of data to be fitted.
start	named list of starting values
method	the method to be used. See Details . Can be abbreviated.
show	logical; if TRUE (the default), print details of the fit.
fpar	a named list with fixed parameters, either scale or shape
warnSE	logical; if TRUE, a warning is printed if the standard errors cannot be returned from the observed information matrix when the shape is less than -0.5.

Value

a list containing the following components:

- estimate a vector containing all the maximum likelihood estimates.
- std.err a vector containing the standard errors.
- vcov the variance covariance matrix, obtained as the numerical inverse of the observed information matrix.
- method the method used to fit the parameter.
- nllh the negative log-likelihood evaluated at the parameter estimate.
- convergence components taken from the list returned by [auglag](#). Values other than 0 indicate that the algorithm likely did not converge.
- counts components taken from the list returned by [auglag](#).
- xdat an n by r matrix of data

Examples

```
xdat <- rrlarg(n = 10, loc = 0, scale = 1, shape = 0.1, r = 4)
fit.rlarg(xdat)
```

fit.shape

Shape parameter estimates

Description

Wrapper to estimate the tail index or shape parameter of an extreme value distribution. Each function has similar sets of arguments, a vector or scalar number of order statistics k and a vector of positive observations $xdat$. The method argument allows users to choose between different indicators, including the Hill estimator (`hill`, for positive observations and shape only), the moment estimator of Dekkers and de Haan (`mom` or `dekkers`), the Beirlant, Vynckier and Teugels generalized quantile estimator (`bvt` or `genquant`), the Pickands estimator (`pickands`), the extreme U -statistics estimator of Oorschot, Segers and Zhou (`osz`, or `pickandsxu`).

Usage

```
fit.shape(
  xdat,
  k,
  method = c("hill", "pickandsxu", "osz", "mom", "dekkers", "bvt", "genquant",
            "pickands"),
  ...
)
```

Arguments

<code>xdat</code>	vector of positive observations of length n
<code>k</code>	number of largest order statistics
<code>method</code>	estimation method.
<code>...</code>	additional parameters passed to functions

Value

a data frame with the number of order statistics k and the shape parameter estimate `shape`, or a single numeric value if k is a scalar.

fit.wgpd	<i>Maximum likelihood estimation for weighted generalized Pareto distribution</i>
----------	---

Description

Weighted maximum likelihood estimation, with user-specified vector of weights.

Usage

```
fit.wgpd(xdat, threshold = 0, weightfun = Stein_weights, ...)
```

Arguments

xdat	vector of observations
threshold	numeric, value of the threshold
weightfun	function whose first argument is the length of the weight vector

Value

a list with components

- estimate a vector containing the scale and shape parameters (optimized and fixed).
- std.err a vector containing the standard errors. For method = "obre", these are Huber's robust standard errors.
- vcov the variance covariance matrix, obtained as the numerical inverse of the observed information matrix. For method = "obre", this is the sandwich Godambe matrix inverse.
- threshold the threshold.
- method the method used to fit the parameter. See details.
- nllh the negative log-likelihood evaluated at the parameter estimate.
- nat number of points lying above the threshold.
- pat proportion of points lying above the threshold.
- convergence logical indicator of convergence.
- weights vector of weights for exceedances.
- exceedances excess over the threshold, sorted in decreasing order.

frwind

French wind data

Description

Daily mean wind speed (in km/h) at four stations in the south of France, namely Cap Cepet (S1), Lyon St-Exupery (S2), Marseille Marignane (S3) and Montelimar (S4). The data includes observations from January 1976 until April 2023; days containing missing values are omitted.

Format

A data frame with 17209 observations and 8 variables:

date date of measurement

S1 wind speed (in km/h) at Cap Cepet

S2 wind speed (in km/h) at Lyon Saint-Exupery

S3 wind speed (in km/h) at Marseille Marignane

S4 wind speed (in km/h) at Montelimar

H2 humidity (in percentage) at Lyon Saint-Exupery

T2 mean temperature (in degree Celcius) at Lyon Saint-Exupery

The metadata attribute includes latitude and longitude (in degrees, minutes, seconds), altitude (in m), station name and station id.

Source

European Climate Assessment and Dataset project <https://www.ecad.eu/>

References

Klein Tank, A.M.G. and Coauthors, 2002. Daily dataset of 20th-century surface air temperature and precipitation series for the European Climate Assessment. *Int. J. of Climatol.*, 22, 1441-1453.

Examples

```
data(frwind, package = "mev")
head(frwind)
attr(frwind, which = "metadata")
```

 geomagnetic

Magnetic storms

Description

Absolute magnitude of 373 geomagnetic storms lasting more than 48h with absolute magnitude (dst) larger than 100 in 1957-2014.

Format

a vector of size 373

Note

For a detailed article presenting the derivation of the Dst index, see <http://wdc.kugi.kyoto-u.ac.jp/dstdir/dst2/onDst>

Source

Aki Vehtari

References

World Data Center for Geomagnetism, Kyoto, M. Nose, T. Iyemori, M. Sugiura, T. Kamei (2015), *Geomagnetic Dst index*, <doi:10.17593/14515-74000>.

 gev

Generalized extreme value distribution

Description

Likelihood, score function and information matrix, bias, approximate ancillary statistics and sample space derivative for the generalized extreme value distribution

Arguments

par	vector of loc, scale and shape
dat	sample vector
method	string indicating whether to use the expected ('exp') or the observed ('obs' - the default) information matrix.
V	vector calculated by gev.vfun
n	sample size
p	vector of probabilities

Usage

```
gev.ll(par, dat)
gev.ll.optim(par, dat)
gev.score(par, dat)
gev.infomat(par, dat, method = c('obs', 'exp'))
gev.retlev(par, p)
gev.bias(par, n)
gev.Fscore(par, dat, method=c('obs', 'exp'))
gev.Vfun(par, dat)
gev.phi(par, dat, V)
gev.dphi(par, dat, V)
```

Functions

- `gev.ll`: log likelihood
- `gev.ll.optim`: negative log likelihood parametrized in terms of location, $\log(\text{scale})$ and shape in order to perform unconstrained optimization
- `gev.score`: score vector
- `gev.infomat`: observed or expected information matrix
- `gev.retlev`: return level, corresponding to the $(1 - p)$ th quantile
- `gev.bias`: Cox-Snell first order bias
- `gev.Fscore`: Firth's modified score equation
- `gev.Vfun`: vector implementing conditioning on approximate ancillary statistics for the TEM
- `gev.phi`: canonical parameter in the local exponential family approximation
- `gev.dphi`: derivative matrix of the canonical parameter in the local exponential family approximation

References

- Firth, D. (1993). Bias reduction of maximum likelihood estimates, *Biometrika*, **80**(1), 27–38.
- Coles, S. (2001). *An Introduction to Statistical Modeling of Extreme Values*, Springer, 209 p.
- Cox, D. R. and E. J. Snell (1968). A general definition of residuals, *Journal of the Royal Statistical Society: Series B (Methodological)*, **30**, 248–275.
- Cordeiro, G. M. and R. Klein (1994). Bias correction in ARMA models, *Statistics and Probability Letters*, **19**(3), 169–176.

 gev.abias

Asymptotic bias of block maxima for fixed sample sizes

Description

Asymptotic bias of block maxima for fixed sample sizes

Usage

```
gev.abias(shape, rho)
```

Arguments

shape	shape parameter
rho	second-order parameter, non-positive

Value

a vector of length three containing the bias for location, scale and shape (in this order)

References

Dombry, C. and A. Ferreira (2017). Maximum likelihood estimators based on the block maxima method. <https://arxiv.org/abs/1705.00465>

 gev.bcor

Bias correction for GEV distribution

Description

Bias corrected estimates for the generalized extreme value distribution using Firth's modified score function or implicit bias subtraction.

Usage

```
gev.bcor(par, dat, corr = c("subtract", "firth"), method = c("obs", "exp"))
```

Arguments

par	parameter vector (scale, shape)
dat	sample of observations
corr	string indicating which correction to employ either subtract or firth
method	string indicating whether to use the expected ('exp') or the observed ('obs' — the default) information matrix. Used only if corr='firth'

Details

Method subtractsolves

$$\tilde{\theta} = \hat{\theta} + b(\tilde{\theta})$$

for $\tilde{\theta}$, using the first order term in the bias expansion as given by `gev.bias`.

The alternative is to use Firth's modified score and find the root of

$$U(\tilde{\theta}) - i(\tilde{\theta})b(\tilde{\theta}),$$

where U is the score vector, b is the first order bias and i is either the observed or Fisher information.

The routine uses the MLE (bias-corrected) as starting values and proceeds to find the solution using a root finding algorithm. Since the bias-correction is not valid for $\xi < -1/3$, any solution that is unbounded will return a vector of NA as the solution does not exist then.

Value

vector of bias-corrected parameters

Examples

```
set.seed(1)
dat <- mev::rgev(n=40, loc = 1, scale=1, shape=-0.2)
par <- mev::fit.gev(dat)$estimate
gev.bcor(par, dat, 'subtract')
gev.bcor(par, dat, 'firth') #observed information
gev.bcor(par, dat, 'firth','exp')
```

gev.mle

Generalized extreme value maximum likelihood estimates for various quantities of interest

Description

This function calls the `fit.gev` routine on the sample of block maxima and returns maximum likelihood estimates for all quantities of interest, including location, scale and shape parameters, quantiles and mean and quantiles of maxima of N blocks.

Usage

```
gev.mle(
  xdat,
  args = c("loc", "scale", "shape", "quant", "Nmean", "Nquant"),
  N,
  p,
  q
)
```

Arguments

xdat	sample vector of maxima
args	vector of strings indicating which arguments to return the maximum likelihood values for.
N	size of block over which to take maxima. Required only for args Nmean and Nquant.
p	tail probability. Required only for arg quant.
q	level of quantile for maxima of N exceedances. Required only for args Nquant.

Value

named vector with maximum likelihood estimated parameter values for arguments args

Examples

```
dat <- mev::rgev(n = 100, shape = 0.2)
gev.mle(xdat = dat, N = 100, p = 0.01, q = 0.5)
```

 gev.Nyr

N-year return levels, median and mean estimate

Description

N-year return levels, median and mean estimate

Usage

```
gev.Nyr(par, nobs, N, type = c("retlev", "median", "mean"), p = 1/N)
```

Arguments

par	vector of location, scale and shape parameters for the GEV distribution
nobs	integer number of observation on which the fit is based
N	integer number of observations for return level. See Details
type	string indicating the statistic to be calculated (can be abbreviated).
p	probability indicating the return level, corresponding to the quantile at $1-1/p$

Details

If there are n_y observations per year, the L-year return level is obtained by taking N equal to $n_y L$.

Value

a list with components

- est point estimate
- var variance estimate based on delta-method
- type statistic

 gev.pll

Profile log-likelihood for the generalized extreme value distribution

Description

This function calculates the profile likelihood along with two small-sample corrections based on Severini's (1999) empirical covariance and the Fraser and Reid tangent exponential model approximation.

Usage

```
gev.pll(
  psi,
  param = c("loc", "scale", "shape", "quant", "Nmean", "Nquant"),
  mod = "profile",
  dat,
  N = NULL,
  p = NULL,
  q = NULL,
  correction = TRUE,
  plot = TRUE,
  ...
)
```

Arguments

psi	parameter vector over which to profile (unidimensional)
param	string indicating the parameter to profile over
mod	string indicating the model, one of profile, tem or modif. See Details .
dat	sample vector
N	size of block over which to take maxima. Required only for param Nmean and Nquant.
p	tail probability. Required only for param quant.
q	probability level of quantile. Required only for param Nquant.
correction	logical indicating whether to use spline.corr to smooth the tem approximation.
plot	logical; should the profile likelihood be displayed? Default to TRUE
...	additional arguments such as output from call to Vfun if mode='tem'.

Details

The two additional mod available are `tem`, the tangent exponential model (TEM) approximation and `modif` for the penalized profile likelihood based on p^* approximation proposed by Severini. For the latter, the penalization is based on the TEM or an empirical covariance adjustment term.

Value

a list with components

- `mle`: maximum likelihood estimate
- `psi.max`: maximum profile likelihood estimate
- `param`: string indicating the parameter to profile over
- `std.error`: standard error of `psi.max`
- `psi`: vector of parameter ψ given in `psi`
- `pll`: values of the profile log likelihood at `psi`
- `maxpll`: value of maximum profile log likelihood

In addition, if `mod` includes `tem`

- `normal`: maximum likelihood estimate and standard error of the interest parameter ψ
- `r`: values of likelihood root corresponding to ψ
- `q`: vector of likelihood modifications
- `rstar`: modified likelihood root vector
- `rstar.old`: uncorrected modified likelihood root vector
- `tem.psimax`: maximum of the tangent exponential model likelihood

In addition, if `mod` includes `modif`

- `tem.mle`: maximum of tangent exponential modified profile log likelihood
- `tem.profl1`: values of the modified profile log likelihood at `psi`
- `tem.maxpll`: value of maximum modified profile log likelihood
- `empcov.mle`: maximum of Severini's empirical covariance modified profile log likelihood
- `empcov.profl1`: values of the modified profile log likelihood at `psi`
- `empcov.maxpll`: value of maximum modified profile log likelihood

References

- Fraser, D. A. S., Reid, N. and Wu, J. (1999), A simple general formula for tail probabilities for frequentist and Bayesian inference. *Biometrika*, **86**(2), 249–264.
- Severini, T. (2000) Likelihood Methods in Statistics. Oxford University Press. ISBN 9780198506508.
- Brazzale, A. R., Davison, A. C. and Reid, N. (2007) Applied asymptotics: case studies in small-sample statistics. Cambridge University Press, Cambridge. ISBN 978-0-521-84703-2

Examples

```
## Not run:
set.seed(123)
dat <- rgev(n = 100, loc = 0, scale = 2, shape = 0.3)
gev.pll(psi = seq(0,0.5, length = 50), param = 'shape', dat = dat)
gev.pll(psi = seq(-1.5, 1.5, length = 50), param = 'loc', dat = dat)
gev.pll(psi = seq(10, 40, length = 50), param = 'quant', dat = dat, p = 0.01)
gev.pll(psi = seq(12, 100, length = 50), param = 'Nmean', N = 100, dat = dat)
gev.pll(psi = seq(12, 90, length = 50), param = 'Nquant', N = 100, dat = dat, q = 0.5)

## End(Not run)
```

 gev.tem

Tangent exponential model approximation for the GEV distribution

Description

The function `gev.tem` provides a tangent exponential model (TEM) approximation for higher order likelihood inference for a scalar parameter for the generalized extreme value distribution. Options include location scale and shape parameters as well as value-at-risk (or return levels). The function attempts to find good values for `psi` that will cover the range of options, but the fail may fit and return an error.

Usage

```
gev.tem(
  param = c("loc", "scale", "shape", "quant", "Nmean", "Nquant"),
  dat,
  psi = NULL,
  p = NULL,
  q = 0.5,
  N = NULL,
  n.psi = 50,
  plot = TRUE,
  correction = TRUE
)
```

Arguments

<code>param</code>	parameter over which to profile
<code>dat</code>	sample vector for the GEV distribution
<code>psi</code>	scalar or ordered vector of values for the interest parameter. If NULL (default), a grid of values centered at the MLE is selected
<code>p</code>	tail probability for the (1-p)th quantile (return levels). Required only if <code>param = 'retlev'</code>
<code>q</code>	probability level of quantile. Required only for <code>param Nquant</code> .

N	size of block over which to take maxima. Required only for param Nmean and Nquant.
n.psi	number of values of psi at which the likelihood is computed, if psi is not supplied (NULL). Odd values are more prone to give rise to numerical instabilities near the MLE. If psi is a vector of length 2 and n.psi is greater than 2, these are taken to be endpoints of the sequence.
plot	logical indicating whether plot.fr should be called upon exit
correction	logical indicating whether spline.corr should be called.

Value

an invisible object of class fr (see tem in package hoa) with elements

- normal: maximum likelihood estimate and standard error of the interest parameter ψ
- par.hat: maximum likelihood estimates
- par.hat.se: standard errors of maximum likelihood estimates
- th.rest: estimated maximum profile likelihood at $(\psi, \hat{\lambda})$
- r: values of likelihood root corresponding to ψ
- psi: vector of interest parameter
- q: vector of likelihood modifications
- rstar: modified likelihood root vector
- rstar.old: uncorrected modified likelihood root vector
- param: parameter

Author(s)

Leo Belzile

Examples

```
## Not run:
set.seed(1234)
dat <- rgev(n = 40, loc = 0, scale = 2, shape = -0.1)
gev.tem('shape', dat = dat, plot = TRUE)
gev.tem('quant', dat = dat, p = 0.01, plot = TRUE)
gev.tem('scale', psi = seq(1, 4, by = 0.1), dat = dat, plot = TRUE)
dat <- rgev(n = 40, loc = 0, scale = 2, shape = 0.2)
gev.tem('loc', dat = dat, plot = TRUE)
gev.tem('Nmean', dat = dat, p = 0.01, N=100, plot = TRUE)
gev.tem('Nquant', dat = dat, q = 0.5, N=100, plot = TRUE)

## End(Not run)
```

gevdist *Generalized extreme value distribution*

Description

Density function, distribution function, quantile function and random number generation for the generalized extreme value distribution.

Usage

```
qgev(p, loc = 0, scale = 1, shape = 0, lower.tail = TRUE, log.p = FALSE)
```

```
rgev(n, loc = 0, scale = 1, shape = 0)
```

```
dgev(x, loc = 0, scale = 1, shape = 0, log = FALSE)
```

```
pgev(q, loc = 0, scale = 1, shape = 0, lower.tail = TRUE, log.p = FALSE)
```

Arguments

p	vector of probabilities
loc	scalar or vector of location parameters whose length matches that of the input
scale	scalar or vector of positive scale parameters whose length matches that of the input
shape	scalar shape parameter
lower.tail	logical; if TRUE (default), returns the distribution function, otherwise the survival function
n	scalar number of observations
x, q	vector of quantiles
log, log.p	logical; if TRUE, probabilities p are given as $\log(p)$.

Details

The distribution function of a GEV distribution with parameters $\text{loc} = \mu$, $\text{scale} = \sigma$ and $\text{shape} = \xi$ is

$$F(x) = \exp\{-[1 + \xi(x - \mu)/\sigma]^{-1/\xi}\}$$

for $1 + \xi(x - \mu)/\sigma > 0$. If $\xi = 0$ the distribution function is defined as the limit as ξ tends to zero.

The quantile function, when evaluated at zero or one, returns the lower and upper endpoint, whether the latter is finite or not.

Author(s)

Leo Belzile, with code adapted from Paul Northrop

References

- Jenkinson, A. F. (1955) The frequency distribution of the annual maximum (or minimum) of meteorological elements. *Quart. J. R. Met. Soc.*, **81**, 158-171. Chapter 3: [doi:10.1002/qj.49708134804](https://doi.org/10.1002/qj.49708134804)
- Coles, S. G. (2001) *An Introduction to Statistical Modeling of Extreme Values*, Springer-Verlag, London. [doi:10.1007/9781447136750_3](https://doi.org/10.1007/9781447136750_3)

gevN	<i>Generalized extreme value distribution (quantile/mean of N-block maxima parametrization)</i>
------	---

Description

Likelihood, score function and information matrix, approximate ancillary statistics and sample space derivative for the generalized extreme value distribution parametrized in terms of the quantiles/mean of N-block maxima parametrization z , scale and shape.

Arguments

par	vector of loc, quantile/mean of N-block maximum and shape
dat	sample vector
V	vector calculated by gevN.Vfun
q	probability, corresponding to q th quantile of the N-block maximum
qty	string indicating whether to calculate the q quantile or the mean

Usage

```

gevN.ll(par, dat, N, q, qty = c('mean', 'quantile'))
gevN.ll.optim(par, dat, N, q = 0.5, qty = c('mean', 'quantile'))
gevN.score(par, dat, N, q = 0.5, qty = c('mean', 'quantile'))
gevN.infomat(par, dat, qty = c('mean', 'quantile'), method = c('obs', 'exp'), N, q = 0.5, nobs = length(dat))
gevN.Vfun(par, dat, N, q = 0.5, qty = c('mean', 'quantile'))
gevN.phi(par, dat, N, q = 0.5, qty = c('mean', 'quantile'), V)
gevN.dphi(par, dat, N, q = 0.5, qty = c('mean', 'quantile'), V)

```

Functions

- gevN.ll: log likelihood
- gevN.score: score vector
- gevN.infomat: expected and observed information matrix
- gevN.Vfun: vector implementing conditioning on approximate ancillary statistics for the TEM
- gevN.phi: canonical parameter in the local exponential family approximation
- gevN.dphi: derivative matrix of the canonical parameter in the local exponential family approximation

Author(s)

Leo Belzile

gevr

*Generalized extreme value distribution (return level parametrization)***Description**

Likelihood, score function and information matrix, approximate ancillary statistics and sample space derivative for the generalized extreme value distribution parametrized in terms of the return level z , scale and shape.

Arguments

par	vector of retlev, scale and shape
dat	sample vector
p	tail probability, corresponding to $(1 - p)$ th quantile for z
method	string indicating whether to use the expected ('exp') or the observed ('obs' - the default) information matrix.
nobs	number of observations
V	vector calculated by <code>gevr.Vfun</code>

Usage

```

gevr.ll(par, dat, p)
gevr.ll.optim(par, dat, p)
gevr.score(par, dat, p)
gevr.infomat(par, dat, p, method = c('obs', 'exp'), nobs = length(dat))
gevr.Vfun(par, dat, p)
gevr.phi(par, dat, p, V)
gevr.dphi(par, dat, p, V)

```

Functions

- `gevr.ll`: log likelihood
- `gevr.ll.optim`: negative log likelihood parametrized in terms of return levels, $\log(\text{scale})$ and shape in order to perform unconstrained optimization
- `gevr.score`: score vector
- `gevr.infomat`: observed information matrix
- `gevr.Vfun`: vector implementing conditioning on approximate ancillary statistics for the TEM
- `gevr.phi`: canonical parameter in the local exponential family approximation
- `gevr.dphi`: derivative matrix of the canonical parameter in the local exponential family approximation

Author(s)

Leo Belzile

gpd

*Generalized Pareto distribution***Description**

Likelihood, score function and information matrix, bias, approximate ancillary statistics and sample space derivative for the generalized Pareto distribution

Arguments

par	vector of scale and shape
dat	sample vector
tol	numerical tolerance for the exponential model
method	string indicating whether to use the expected ('exp') or the observed ('obs' - the default) information matrix.
V	vector calculated by <code>gpd.Vfun</code>
n	sample size

Usage

```
gpd.ll(par, dat, tol=1e-5)
gpd.ll.optim(par, dat, tol=1e-5)
gpd.score(par, dat)
gpd.infomat(par, dat, method = c('obs', 'exp'))
gpd.bias(par, n)
gpd.Fscore(par, dat, method = c('obs', 'exp'))
gpd.Vfun(par, dat)
gpd.phi(par, dat, V)
gpd.dphi(par, dat, V)
```

Functions

- `gpd.ll`: log likelihood
- `gpd.ll.optim`: negative log likelihood parametrized in terms of $\log(\text{scale})$ and shape in order to perform unconstrained optimization
- `gpd.score`: score vector
- `gpd.infomat`: observed or expected information matrix
- `gpd.bias`: Cox-Snell first order bias
- `gpd.Fscore`: Firth's modified score equation
- `gpd.Vfun`: vector implementing conditioning on approximate ancillary statistics for the TEM
- `gpd.phi`: canonical parameter in the local exponential family approximation
- `gpd.dphi`: derivative matrix of the canonical parameter in the local exponential family approximation

Author(s)

Leo Belzile

References

- Firth, D. (1993). Bias reduction of maximum likelihood estimates, *Biometrika*, **80**(1), 27–38.
- Coles, S. (2001). *An Introduction to Statistical Modeling of Extreme Values*, Springer, 209 p.
- Cox, D. R. and E. J. Snell (1968). A general definition of residuals, *Journal of the Royal Statistical Society: Series B (Methodological)*, **30**, 248–275.
- Cordeiro, G. M. and R. Klein (1994). Bias correction in ARMA models, *Statistics and Probability Letters*, **19**(3), 169–176.
- Giles, D. E., Feng, H. and R. T. Godwin (2016). Bias-corrected maximum likelihood estimation of the parameters of the generalized Pareto distribution, *Communications in Statistics - Theory and Methods*, **45**(8), 2465–2483.

gpd.abias

*Asymptotic bias of threshold exceedances for k order statistics***Description**

The formula given in de Haan and Ferreira, 2007 (Springer). Note that the latter differs from that found in Drees, Ferreira and de Haan.

Usage

```
gpd.abias(shape, rho)
```

Arguments

shape	shape parameter
rho	second-order parameter, non-positive

Value

a vector of length containing the bias for scale and shape (in this order)

References

- Dombry, C. and A. Ferreira (2017). Maximum likelihood estimators based on the block maxima method. <https://arxiv.org/abs/1705.00465>

gpd.bcor

*Bias correction for GP distribution***Description**

Bias corrected estimates for the generalized Pareto distribution using Firth's modified score function or implicit bias subtraction.

Usage

```
gpd.bcor(par, dat, corr = c("subtract", "firth"), method = c("obs", "exp"))
```

Arguments

par	parameter vector (scale, shape)
dat	sample of observations
corr	string indicating which correction to employ either subtract or firth
method	string indicating whether to use the expected ('exp') or the observed ('obs' — the default) information matrix. Used only if corr='firth'

Details

Method subtract solves

$$\tilde{\theta} = \hat{\theta} + b(\tilde{\theta})$$

for $\tilde{\theta}$, using the first order term in the bias expansion as given by [gpd.bias](#).

The alternative is to use Firth's modified score and find the root of

$$U(\tilde{\theta}) - i(\tilde{\theta})b(\tilde{\theta}),$$

where U is the score vector, b is the first order bias and i is either the observed or Fisher information.

The routine uses the MLE as starting value and proceeds to find the solution using a root finding algorithm. Since the bias-correction is not valid for $\xi < -1/3$, any solution that is unbounded will return a vector of NA as the bias correction does not exist then.

Value

vector of bias-corrected parameters

Examples

```
set.seed(1)
dat <- rgp(n=40, scale=1, shape=-0.2)
par <- gp.fit(dat, threshold=0, show=FALSE)$estimate
gpd.bcor(par,dat, 'subtract')
gpd.bcor(par,dat, 'firth') #observed information
gpd.bcor(par,dat, 'firth','exp')
```

gpd.boot	<i>Bootstrap approximation for generalized Pareto parameters</i>
----------	--

Description

Given an object of class `mev_gpd`, returns a matrix of parameter values to mimic the estimation uncertainty.

Usage

```
gpd.boot(object, B = 1000L, method = c("post", "norm"))
```

Arguments

object	object of class <code>mev_gpd</code>
B	number of pairs to sample
method	string; one of 'norm' for the normal approximation or 'post' (default) for posterior sampling

Details

Two options are available: a normal approximation to the scale and shape based on the maximum likelihood estimates and the observed information matrix. This method uses forward sampling to simulate from a bivariate normal distribution that satisfies the support and positivity constraints

The second approximation uses the ratio-of-uniforms method to obtain samples from the posterior distribution with uninformative priors, thus mimicking the joint distribution of maximum likelihood. The benefit of the latter is that it is more reliable in small samples and when the shape is negative.

Value

a matrix of size B by 2 whose columns contain scale and shape parameters

gpd.mle	<i>Generalized Pareto maximum likelihood estimates for various quantities of interest</i>
---------	---

Description

This function calls the `fit.gpd` routine on the sample of excesses and returns maximum likelihood estimates for all quantities of interest, including scale and shape parameters, quantiles and value-at-risk, expected shortfall and mean and quantiles of maxima of N threshold exceedances

Usage

```
gpd.mle(
  xdat,
  args = c("scale", "shape", "quant", "VaR", "ES", "Nmean", "Nquant"),
  m,
  N,
  p,
  q
)
```

Arguments

xdat	sample vector of excesses
args	vector of strings indicating which arguments to return the maximum likelihood values for
m	number of observations of interest for return levels. Required only for args values 'VaR' or 'ES'
N	size of block over which to take maxima. Required only for args Nmean and Nquant.
p	tail probability, equivalent to $1/m$. Required only for args quant.
q	level of quantile for N-block maxima. Required only for args Nquant.

Value

named vector with maximum likelihood values for arguments args

Examples

```
xdat <- mev::rgp(n = 30, shape = 0.2)
gpd.mle(xdat = xdat, N = 100, p = 0.01, q = 0.5, m = 100)
```

gpd.pll

Profile log-likelihood for the generalized Pareto distribution

Description

This function calculates the (modified) profile likelihood based on the p^* formula. There are two small-sample corrections that use a proxy for $\ell_{\lambda;\hat{\lambda}}$, which are based on Severini's (1999) empirical covariance and the Fraser and Reid tangent exponential model approximation.

Usage

```

gpd.pll(
  psi,
  param = c("scale", "shape", "quant", "VaR", "ES", "Nmean", "Nquant"),
  mod = "profile",
  mle = NULL,
  dat,
  m = NULL,
  N = NULL,
  p = NULL,
  q = NULL,
  correction = TRUE,
  threshold = NULL,
  plot = TRUE,
  ...
)

```

Arguments

<code>psi</code>	parameter vector over which to profile (unidimensional)
<code>param</code>	string indicating the parameter to profile over
<code>mod</code>	string indicating the model. See Details .
<code>mle</code>	maximum likelihood estimate in (ψ, ξ) parametrization if $\psi \neq \xi$ and (σ, ξ) otherwise (optional).
<code>dat</code>	sample vector of excesses, unless <code>threshold</code> is provided (in which case user provides original data)
<code>m</code>	number of observations of interest for return levels. Required only for args values 'VaR' or 'ES'
<code>N</code>	size of block over which to take maxima. Required only for args <code>Nmean</code> and <code>Nquant</code> .
<code>p</code>	tail probability, equivalent to $1/m$. Required only for args <code>quant</code> .
<code>q</code>	level of quantile for N-block maxima. Required only for args <code>Nquant</code> .
<code>correction</code>	logical indicating whether to use <code>spline.corr</code> to smooth the tem approximation.
<code>threshold</code>	numerical threshold above which to fit the generalized Pareto distribution
<code>plot</code>	logical; should the profile likelihood be displayed? Default to TRUE
<code>...</code>	additional arguments such as output from call to <code>Vfun</code> if <code>mode='tem'</code> .

Details

The three `mod` available are `profile` (the default), `tem`, the tangent exponential model (TEM) approximation and `modif` for the penalized profile likelihood based on p^* approximation proposed by Severini. For the latter, the penalization is based on the TEM or an empirical covariance adjustment term.

Value

a list with components

- `mle`: maximum likelihood estimate
- `psi.max`: maximum profile likelihood estimate
- `param`: string indicating the parameter to profile over
- `std.error`: standard error of `psi.max`
- `psi`: vector of parameter ψ given in `psi`
- `pll`: values of the profile log likelihood at `psi`
- `maxpll`: value of maximum profile log likelihood
- `family`: a string indicating "gpd"
- `threshold`: value of the threshold, by default zero

In addition, if `mod` includes `tem`

- `normal`: maximum likelihood estimate and standard error of the interest parameter ψ
- `r`: values of likelihood root corresponding to ψ
- `q`: vector of likelihood modifications
- `rstar`: modified likelihood root vector
- `rstar.old`: uncorrected modified likelihood root vector
- `tem.psimax`: maximum of the tangent exponential model likelihood

In addition, if `mod` includes `modif`

- `tem.mle`: maximum of tangent exponential modified profile log likelihood
- `tem.profl1`: values of the modified profile log likelihood at `psi`
- `tem.maxpll`: value of maximum modified profile log likelihood
- `empcov.mle`: maximum of Severini's empirical covariance modified profile log likelihood
- `empcov.profl1`: values of the modified profile log likelihood at `psi`
- `empcov.maxpll`: value of maximum modified profile log likelihood

Examples

```
## Not run:
dat <- rgp(n = 100, scale = 2, shape = 0.3)
gpd.pll(psi = seq(-0.5, 1, by=0.01), param = 'shape', dat = dat)
gpd.pll(psi = seq(0.1, 5, by=0.1), param = 'scale', dat = dat)
gpd.pll(psi = seq(20, 35, by=0.1), param = 'quant', dat = dat, p = 0.01)
gpd.pll(psi = seq(20, 80, by=0.1), param = 'ES', dat = dat, m = 100)
gpd.pll(psi = seq(15, 100, by=1), param = 'Nmean', N = 100, dat = dat)
gpd.pll(psi = seq(15, 90, by=1), param = 'Nquant', N = 100, dat = dat, q = 0.5)

## End(Not run)
```


Description

The function `gpd.tem` provides a tangent exponential model (TEM) approximation for higher order likelihood inference for a scalar parameter for the generalized Pareto distribution. Options include scale and shape parameters as well as value-at-risk (also referred to as quantiles, or return levels) and expected shortfall. The function attempts to find good values for `psi` that will cover the range of options, but the fit may fail and return an error. In such cases, the user can try to find good grid of starting values and provide them to the routine.

Usage

```
gpd.tem(
  dat,
  param = c("scale", "shape", "quant", "VaR", "ES", "Nmean", "Nquant"),
  psi = NULL,
  m = NULL,
  threshold = 0,
  n.psi = 50,
  N = NULL,
  p = NULL,
  q = NULL,
  plot = FALSE,
  correction = TRUE
)
```

Arguments

<code>dat</code>	sample vector for the GP distribution
<code>param</code>	parameter over which to profile
<code>psi</code>	scalar or ordered vector of values for the interest parameter. If <code>NULL</code> (default), a grid of values centered at the MLE is selected. If <code>psi</code> is of length 2 and <code>n.psi</code> >2, it is assumed to be the minimal and maximal values at which to evaluate the profile log likelihood.
<code>m</code>	number of observations of interest for return levels. See Details . Required only for <code>param = 'VaR'</code> or <code>param = 'ES'</code> .
<code>threshold</code>	threshold value corresponding to the lower bound of the support or the location parameter of the generalized Pareto distribution.
<code>n.psi</code>	number of values of <code>psi</code> at which the likelihood is computed, if <code>psi</code> is not supplied (<code>NULL</code>). Odd values are more prone to give rise to numerical instabilities near the MLE
<code>N</code>	size of block over which to take maxima. Required only for args <code>Nmean</code> and <code>Nquant</code> .

p	tail probability, equivalent to $1/m$. Required only for args quant.
q	level of quantile for N-block maxima. Required only for args Nquant.
plot	logical indicating whether plot.fr should be called upon exit
correction	logical indicating whether spline.corr should be called.

Details

As of version 1.11, this function is a wrapper around `gpd.pll`.

The interpretation for m is as follows: if there are on average m_y observations per year above the threshold, then $m = Tm_y$ corresponds to T -year return level.

Value

an invisible object of class `fr` (see `tem` in package `hoa`) with elements

- `normal`: maximum likelihood estimate and standard error of the interest parameter ψ
- `par.hat`: maximum likelihood estimates
- `par.hat.se`: standard errors of maximum likelihood estimates
- `th.rest`: estimated maximum profile likelihood at $(\psi, \hat{\lambda})$
- `r`: values of likelihood root corresponding to ψ
- `psi`: vector of interest parameter
- `q`: vector of likelihood modifications
- `rstar`: modified likelihood root vector
- `rstar.old`: uncorrected modified likelihood root vector
- `param`: parameter

Author(s)

Leo Belzile

Examples

```
set.seed(123)
dat <- rgp(n = 40, scale = 1, shape = -0.1)
#with plots
m1 <- gpd.tem(param = 'shape', n.psi = 50, dat = dat, plot = TRUE)
## Not run:
m2 <- gpd.tem(param = 'scale', n.psi = 50, dat = dat)
m3 <- gpd.tem(param = 'VaR', n.psi = 50, dat = dat, m = 100)
#Providing psi
psi <- c(seq(2, 5, length = 15), seq(5, 35, length = 45))
m4 <- gpd.tem(param = 'ES', dat = dat, m = 100, psi = psi, correction = FALSE)
mev:::plot.fr(m4, which = c(2, 4))
plot(fr4 <- spline.corr(m4))
confint(m1)
confint(m4, parm = 2, warn = FALSE)
m5 <- gpd.tem(param = 'Nmean', dat = dat, N = 100, psi = psi, correction = FALSE)
```

```
m6 <- gpd.tem(param = 'Nquant', dat = dat, N = 100, q = 0.7, correction = FALSE)

## End(Not run)
```

gpde

Generalized Pareto distribution (expected shortfall parametrization)

Description

Likelihood, score function and information matrix, approximate ancillary statistics and sample space derivative for the generalized Pareto distribution parametrized in terms of expected shortfall.

The parameter m corresponds to $\zeta_u/(1-\alpha)$, where ζ_u is the rate of exceedance over the threshold u and α is the percentile of the expected shortfall. Note that the actual parametrization is in terms of excess expected shortfall, meaning expected shortfall minus threshold.

Arguments

par	vector of length 2 containing e_m and ξ , respectively the expected shortfall at probability $1/(1-\alpha)$ and the shape parameter.
dat	sample vector
m	number of observations of interest for return levels. See Details
tol	numerical tolerance for the exponential model
method	string indicating whether to use the expected ('exp') or the observed ('obs' - the default) information matrix.
nobs	number of observations
V	vector calculated by <code>gpde.Vfun</code>

Details

The observed information matrix was calculated from the Hessian using symbolic calculus in Sage.

Usage

```
gpde.ll(par, dat, m, tol=1e-5)
gpde.ll.optim(par, dat, m, tol=1e-5)
gpde.score(par, dat, m)
gpde.infomat(par, dat, m, method = c('obs', 'exp'), nobs = length(dat))
gpde.Vfun(par, dat, m)
gpde.phi(par, dat, V, m)
gpde.dphi(par, dat, V, m)
```

Functions

- `gpde.ll`: log likelihood
- `gpde.ll.optim`: negative log likelihood parametrized in terms of log expected shortfall and shape in order to perform unconstrained optimization
- `gpde.score`: score vector
- `gpde.infomat`: observed information matrix for GPD parametrized in terms of rate of expected shortfall and shape
- `gpde.Vfun`: vector implementing conditioning on approximate ancillary statistics for the TEM
- `gpde.phi`: canonical parameter in the local exponential family approximation
- `gpde.dphi`: derivative matrix of the canonical parameter in the local exponential family approximation

Author(s)

Leo Belzile

gpdist

Generalized Pareto distribution

Description

Density function, distribution function, quantile function and random number generation for the generalized Pareto distribution.

Usage

```
pgp(q, loc = 0, scale = 1, shape = 0, lower.tail = TRUE, log.p = FALSE)
```

```
dgp(x, loc = 0, scale = 1, shape = 0, log = FALSE)
```

```
qgp(p, loc = 0, scale = 1, shape = 0, lower.tail = TRUE)
```

```
rgp(n, loc = 0, scale = 1, shape = 0)
```

Arguments

<code>loc</code>	location parameter.
<code>scale</code>	scale parameter, strictly positive.
<code>shape</code>	shape parameter.
<code>lower.tail</code>	logical; if TRUE (default), the lower tail probability $\Pr(X \leq x)$ is returned.
<code>log.p, log</code>	logical; if FALSE (default), values are returned on the probability scale.
<code>x, q</code>	vector of quantiles
<code>p</code>	vector of probabilities
<code>n</code>	scalar number of observations

References

Coles, S. G. (2001) *An Introduction to Statistical Modeling of Extreme Values*, Springer-Verlag, London. doi:[10.1007/9781447136750_3](https://doi.org/10.1007/9781447136750_3)

gpdN	<i>Generalized Pareto distribution (mean of maximum of N exceedances parametrization)</i>
------	---

Description

Likelihood, score function and information matrix, approximate ancillary statistics and sample space derivative for the generalized Pareto distribution parametrized in terms of average maximum of N exceedances.

The parameter N corresponds to the number of threshold exceedances of interest over which the maxima is taken. z is the corresponding expected value of this block maxima. Note that the actual parametrization is in terms of excess expected mean, meaning expected mean minus threshold.

Arguments

par	vector of length 2 containing z and ξ , respectively the mean excess of the maxima of N exceedances above the threshold and the shape parameter.
dat	sample vector
N	block size for threshold exceedances.
tol	numerical tolerance for the exponential model
V	vector calculated by gpdN.Vfun

Details

The observed information matrix was calculated from the Hessian using symbolic calculus in Sage.

Usage

```
gpdN.ll(par, dat, N, tol=1e-5)
gpdN.score(par, dat, N)
gpdN.infomat(par, dat, N, method = c('obs', 'exp'), nobs = length(dat))
gpdN.Vfun(par, dat, N)
gpdN.phi(par, dat, N, V)
gpdN.dphi(par, dat, N, V)
```

Functions

- gpdN.ll: log likelihood
- gpdN.score: score vector
- gpdN.infomat: observed information matrix for GP parametrized in terms of mean of the maximum of N exceedances and shape

- `gpdN.Vfun`: vector implementing conditioning on approximate ancillary statistics for the TEM
- `gpdN.phi`: canonical parameter in the local exponential family approximation
- `gpdN.dphi`: derivative matrix of the canonical parameter in the local exponential family approximation

Author(s)

Leo Belzile

gpd

Generalized Pareto distribution (return level parametrization)

Description

Likelihood, score function and information matrix, approximate ancillary statistics and sample space derivative for the generalized Pareto distribution parametrized in terms of return levels.

Arguments

<code>par</code>	vector of length 2 containing y_m and ξ , respectively the m -year return level and the shape parameter.
<code>dat</code>	sample vector
<code>m</code>	number of observations of interest for return levels. See Details
<code>tol</code>	numerical tolerance for the exponential model
<code>method</code>	string indicating whether to use the expected ('exp') or the observed ('obs' - the default) information matrix.
<code>nobs</code>	number of observations
<code>V</code>	vector calculated by <code>gpd.Vfun</code>

Details

The observed information matrix was calculated from the Hessian using symbolic calculus in Sage.

The interpretation for m is as follows: if there are on average m_y observations per year above the threshold, then $m = Tm_y$ corresponds to T -year return level.

Usage

```
gpd.ll(par, dat, m, tol=1e-5)
gpd.ll.optim(par, dat, m, tol=1e-5)
gpd.score(par, dat, m)
gpd.informat(par, dat, m, method = c('obs', 'exp'), nobs = length(dat))
gpd.Vfun(par, dat, m)
gpd.phi(par, V, dat, m)
gpd.dphi(par, V, dat, m)
```

Functions

- `gpd. ll`: log likelihood
- `gpd. ll. optim`: negative log likelihood parametrized in terms of $\log(\text{scale})$ and shape in order to perform unconstrained optimization
- `gpd. score`: score vector
- `gpd. infomat`: observed information matrix for GPD parametrized in terms of rate of m -year return level and shape
- `gpd. Vfun`: vector implementing conditioning on approximate ancillary statistics for the TEM
- `gpd. phi`: canonical parameter in the local exponential family approximation
- `gpd. dphi`: derivative matrix of the canonical parameter in the local exponential family approximation

Author(s)

Leo Belzile

ibvpot

Interpret bivariate threshold exceedance models

Description

This is an adaptation of the `evir` package `interpret.gpdbiv` function. `interpret.fbvpot` deals with the output of a call to `fbvpot` from the **evd** and to handle families other than the logistic distribution. The likelihood derivation comes from expression 2.10 in Smith et al. (1997).

Usage

```
ibvpot(fitted, q, silent = FALSE)
```

Arguments

<code>fitted</code>	the output of <code>fbvpot</code> or a list. See Details.
<code>q</code>	a vector of quantiles to consider, on the data scale. Must be greater than the thresholds.
<code>silent</code>	boolean; whether to print the interpretation of the result. Default to FALSE.

Details

The list `fitted` must contain

- `model` a string; see `bvevd` from package `evd` for options
- `param` a named vector containing the parameters of the model, as well as parameters `scale1`, `shape1`, `scale2` and `shape2`, corresponding to marginal GPD parameters.
- `threshold` a vector of length 2 containing the two thresholds.
- `pat` the proportion of observations above the corresponding threshold

Value

an invisible numeric vector containing marginal, joint and conditional exceedance probabilities.

Author(s)

Leo Belzile, adapting original S code by Alexander McNeil

References

Smith, Tawn and Coles (1997), Markov chain models for threshold exceedances. *Biometrika*, **84**(2), 249–268.

See Also

interpret.gpdbiv in package evir

Examples

```
if (requireNamespace("evd", quietly = TRUE)) {
  y <- rgp(1000,1,1,1)
  x <- y*rmevspec(n=1000,d=2,sigma=cbind(c(0,0.5),c(0.5,0)), model='hr')
  mod <- evd::fbvpot(x, threshold = c(1,1), model = 'hr', likelihood = 'censored')
  ibvpot(mod, c(20,20))
}
```

infomat.test

Information matrix test statistic and MLE for the extremal index

Description

The Information Matrix Test (IMT), proposed by Suveges and Davison (2010), is based on the difference between the expected quadratic score and the second derivative of the log-likelihood. The asymptotic distribution for each threshold u and gap K is asymptotically χ^2 with one degree of freedom. The approximation is good for $N > 80$ and conservative for smaller sample sizes. The test assumes independence between gaps.

Usage

```
infomat.test(xdat, thresh, q, K, plot = TRUE, ...)
```

Arguments

xdat	data vector
thresh	threshold vector
q	vector of probability levels to define threshold if thresh is missing.
K	int specifying the largest K-gap
plot	logical: should the graphical diagnostic be plotted?
...	additional arguments, currently ignored

Details

The procedure proposed in Suveges & Davison (2010) was corrected for erratas. The maximum likelihood is based on the limiting mixture distribution of the intervals between exceedances (an exponential with a point mass at zero). The condition $D^{(K)}(u_n)$ should be checked by the user.

Fukutome et al. (2015) propose an ad hoc automated procedure

1. Calculate the interexceedance times for each K-gap and each threshold, along with the number of clusters
2. Select the (u, K) pairs for which $IMT < 0.05$ (corresponding to a P-value of 0.82)
3. Among those, select the pair (u, K) for which the number of clusters is the largest

Value

an invisible list of matrices containing

- IMT a matrix of test statistics
- pvals a matrix of approximate p-values (corresponding to probabilities under a χ_1^2 distribution)
- mle a matrix of maximum likelihood estimates for each given pair (u, K)
- loglik a matrix of log-likelihood values at MLE for each given pair (u, K)
- threshold a vector of thresholds based on empirical quantiles at supplied levels.
- q the vector q supplied by the user
- K the largest gap number, supplied by the user

Author(s)

Leo Belzile

References

Fukutome, Liniger and Suveges (2015), Automatic threshold and run parameter selection: a climatology for extreme hourly precipitation in Switzerland. *Theoretical and Applied Climatology*, **120**(3), 403-416.

Suveges and Davison (2010), Model misspecification in peaks over threshold analysis. *Annals of Applied Statistics*, **4**(1), 203-221.

White (1982), Maximum Likelihood Estimation of Misspecified Models. *Econometrica*, **50**(1), 1-25.

Examples

```
infomat.test(xdat = rgp(n = 10000),
             q = seq(0.1, 0.9, length = 10),
             K = 3)
```

lambdadep	<i>Estimation of the bivariate angular dependence function of Wadsworth and Tawn (2013)</i>
-----------	---

Description

Estimation of the bivariate angular dependence function of Wadsworth and Tawn (2013)

Usage

```
lambdadep(dat, qu = 0.95, method = c("hill", "mle", "bayes"), plot = TRUE)
```

Arguments

dat	an n by 2 matrix of multivariate observations
qu	quantile level on uniform scale at which to threshold data. Default to 0.95
method	string indicating the estimation method
plot	logical indicating whether to return the graph of lambda The confidence intervals are based on normal quantiles. The standard errors for the hill are based on the asymptotic covariance and that of the mle derived using the delta-method. Bayesian posterior predictive interval estimates are obtained using ratio-of-uniform sampling with flat priors: the shape parameters are constrained to lie within the triangle, as are frequentist point estimates which are adjusted post-inference.

Value

a plot of the lambda function if plot=TRUE, plus an invisible list with components

- w the sequence of angles in (0,1) at which the lambda values are evaluated
- lambda point estimates of lambda
- lower.confint 95
- upper.confint 95

Examples

```
set.seed(12)
dat <- mev::rmev(n = 1000, d = 2, model = "log", param = 0.1)
lambdadep(dat, method = 'hill')
## Not run:
lambdadep(dat, method = 'bayes')
lambdadep(dat, method = 'mle')
# With independent observations
dat <- matrix(runif(n = 2000), ncol = 2)
lambdadep(dat, method = 'hill')

## End(Not run)
```

likmgp

*Likelihood for multivariate peaks over threshold models***Description**

Likelihood for the various parametric limiting models over region determined by

$$\{y \in F : \max_{j=1}^D \sigma_j \frac{y_j^\xi - 1}{\xi_j} + \mu_j > u\};$$

where μ is loc, σ is scale and ξ is shape.

Usage

```
likmgp(
  dat,
  thresh,
  loc,
  scale,
  shape,
  par,
  model = c("log", "br", "xstud"),
  likt = c("mgp", "pois", "binom"),
  lambdau = 1,
  ...
)
```

Arguments

dat	matrix of observations
thresh	functional threshold for the maximum
loc	vector of location parameter for the marginal generalized Pareto distribution
scale	vector of scale parameter for the marginal generalized Pareto distribution
shape	vector of shape parameter for the marginal generalized Pareto distribution
par	list of parameters: alpha for the logistic model, Lambda for the Brown–Resnick model or else Sigma and df for the extremal Student.
model	string indicating the model family, one of "log", "neglog", "br" or "xstud"
likt	string indicating the type of likelihood, with an additional contribution for the non-exceeding components: one of "mgp", "binom" and "pois".
lambdau	vector of marginal rate of marginal threshold exceedance.
...	additional arguments (see Details)

Details

Optional arguments can be passed to the function via . . .

- c1 cluster instance created by makeCluster (default to NULL)
- ncores number of cores for parallel computing of the likelihood
- mmax maximum per column
- B1 number of replicates for quasi Monte Carlo integral for the exponent measure
- genvec1 generating vector for the quasi Monte Carlo routine (exponent measure), associated with B1

Value

the value of the log-likelihood with attributes expme, giving the exponent measure

Note

The location and scale parameters are not identifiable unless one of them is fixed.

maiquetia

Maiquetia Daily Rainfall

Description

Daily cumulated rainfall (in mm) at Maiquetia airport, Venezuela. The observations cover the period from January 1961 to December 1999. The original series had missing days in February 1996 (during which there were 2 days with 1hr each of light rain) and January 1998 (no rain). These were replaced by zeros.

Format

a vector of size 14244 containing daily rainfall (in mm),

Source

J.R. Cordova and M. González, accessed 25.11.2018 from <<https://rss.onlinelibrary.wiley.com/hub/journal/14679876/series-c-datasets>>

References

- Coles, S. and L.R. Pericchi (2003). Anticipating Catastrophes through Extreme Value Modelling, *Applied Statistics*, **52**(4), 405-416.
- Coles, S., Pericchi L.R. and S. Sisson (2003). A fully probabilistic approach to extreme rainfall modeling, *Journal of Hydrology*, **273**, 35-50.

Examples

```
## Not run:
data(maiquetia, package = "mev")
day <- seq.Date(from = as.Date("1961-01-01"), to = as.Date("1999-12-31"), by = "day")
nzrain <- maiquetia[substr(day, 1, 4) < 1999 & maiquetia > 0]
fit.gpd(nzrain, threshold = 30, show = TRUE)

## End(Not run)
```

maxstabtest

P-P plot for testing max stability

Description

The diagnostic, proposed by Gabda, Towe, Wadsworth and Tawn, relies on the fact that, for max-stable vectors on the unit Gumbel scale, the distribution of the maxima is Gumbel distribution with a location parameter equal to the exponent measure. One can thus consider tuples of size m and estimate the location parameter via maximum likelihood and transforming observations to the standard Gumbel scale. Replicates are then pooled and empirical quantiles are defined. The number of combinations of m vectors can be prohibitively large, hence only n_{\max} randomly selected tuples are selected from all possible combinations. The confidence intervals are obtained by a nonparametric bootstrap, by resampling observations with replacement observations for the selected tuples and re-estimating the location parameter. The procedure can be computationally intensive as a result.

Usage

```
maxstabtest(
  dat,
  m = prod(dim(dat)[-1]),
  nmax = 500L,
  B = 1000L,
  ties.method = "random",
  plot = TRUE
)
```

Arguments

<code>dat</code>	matrix or array of max-stable observations, typically block maxima. The first dimension should consist of replicates
<code>m</code>	integer indicating how many tuples should be aggregated.
<code>nmax</code>	maximum number of pairs. Default to 500L.
<code>B</code>	number of nonparametric bootstrap replications. Default to 1000L.
<code>ties.method</code>	string indicating the method for rank . Default to "random".
<code>plot</code>	logical indicating whether a graph should be produced (default to TRUE).

Value

a Tukey probability-probability plot with 95

References

Gabda, D.; Towe, R. Wadsworth, J. and J. Tawn, Discussion of “Statistical Modeling of Spatial Extremes” by A. C. Davison, S. A. Padoan and M. Ribatet. *Statist. Sci.* **27** (2012), no. 2, 189–192.

Examples

```
## Not run:
dat <- mev::rmev(n = 250, d = 100, param = 0.5, model = "log")
maxstabtest(dat, m = 100)
maxstabtest(dat, m = 2, nmax = 100)
dat <- mev::mvrnorm(n = 250, Sigma = diag(0.5, 10) + matrix(0.5, 10, 10), mu = rep(0, 10))
maxstabtest(dat, m = 2, nmax = 100)
maxstabtest(dat, m = ncol(dat))

## End(Not run)
```

mvrnorm

Multivariate Normal distribution sampler

Description

Sampler derived using the eigendecomposition of the covariance matrix Sigma. The function uses the Armadillo random normal generator

Usage

```
mvrnorm(n, mu, Sigma)
```

Arguments

n	sample size
mu	mean vector. Will set the dimension
Sigma	a square covariance matrix, of same dimension as mu. No sanity check is performed to validate that the matrix is p.s.d., so use at own risk

Value

an n sample from a multivariate Normal distribution

Examples

```
mvrnorm(n=10, mu=c(0,2), Sigma=diag(2))
```

NC.diag	<i>Score and likelihood ratio tests fit of equality of shape over multiple thresholds</i>
---------	---

Description

The function returns a P-value path for the score test and/or likelihood ratio test for equality of the shape parameters over multiple thresholds under the generalized Pareto model.

Usage

```
NC.diag(
  xdat,
  u,
  GP.fit = c("Grimshaw", "nlm", "optim", "ismev"),
  do.LRT = FALSE,
  size = NULL,
  plot = TRUE,
  ...,
  xi.tol = 0.001
)
```

Arguments

<code>xdat</code>	numeric vector of raw data
<code>u</code>	m-vector of thresholds (sorted from smallest to largest)
<code>GP.fit</code>	function used to optimize the generalized Pareto model.
<code>do.LRT</code>	boolean indicating whether to perform the likelihood ratio test (in addition to the score test)
<code>size</code>	level at which a horizontal line is drawn on multiple threshold plot
<code>plot</code>	logical; if TRUE, return a plot of p-values against threshold.
<code>...</code>	additional parameters passed to plot
<code>xi.tol</code>	numerical tolerance for threshold distance; if the absolute value of <code>xi1.hat</code> is less than <code>xi.tol</code> use linear interpolation to evaluate score vectors, expected Fisher information matrices, Hessians

Details

The default method is 'Grimshaw' using the reduction of the parameters to a one-dimensional maximization. Other options are one-dimensional maximization of the profile the `nlm` function or `optim`. Two-dimensional optimisation using 2D-optimization `ismev` using the routine from `gpd.fit` from the `ismev` library, with the addition of the algebraic gradient. The choice of `GP.fit` should make no difference but the options were kept. **Warning:** the function will not recover from failure of the maximization routine, returning various error messages.

Value

a plot of P-values for the test at the different thresholds u

Author(s)

Paul J. Northrop and Claire L. Coleman

References

Grimshaw (1993). Computing Maximum Likelihood Estimates for the Generalized Pareto Distribution, *Technometrics*, **35**(2), 185–191.

Northrop & Coleman (2014). Improved threshold diagnostic plots for extreme value analyses, *Extremes*, **17**(2), 289–303.

Wadsworth & Tawn (2012). Likelihood-based procedures for threshold diagnostics and uncertainty in extreme value modelling, *J. R. Statist. Soc. B*, **74**(3), 543–567.

Examples

```
## Not run:
data(nidd)
u <- seq(65,90, by = 1L)
NC.diag(nidd, u, size = 0.05)

## End(Not run)
```

nidd

River Nidd Flow

Description

The data consists of exceedances over the threshold 65 cubic meter per second of the River Nidd at Hunsingore Weir, for 35 years of data between 1934 and 1969.

Format

a vector of size 154

Source

Natural Environment Research Council (1975). *Flood Studies Report*, volume 4. pp. 235–236.

References

Davison, A.C. and R.L. Smith (1990). Models for Exceedances over High Thresholds, *Journal of the Royal Statistical Society. Series B (Methodological)*, **52**(3), 393–442. With discussion.

See Also

nidd.thresh from the evir package

nutrients

Nutrient data

Description

Interview component of survey 'What we eat in America'. These are extracted from the 2015–2016 National Health and Nutrition Examination Survey (NHANES, <https://wwwn.cdc.gov/nchs/nhanes/Default.aspx>) report and consist of the total nutrients for all food and beverage intake ingested over a 24 hours period.

Usage

nutrients

Format

A data frame with 9544 rows and 38 variables:

prot proteins (in grams)
carb carbohydrate (in gram)
sugr total sugars (in gram)
fibe dietary fibers (in grams)
tfat total fat (in grams)
sfat saturated fat (in grams)
mfat monounsaturated fat (in grams)
pfat polyunsaturated fat (in grams)
chol cholesterol (in milligrams)
atoc vitamin E as alpha-tocopherol (in milligrams)
ret retinol (in micrograms)
vara Vitamin A as retinol activity equivalents (in micrograms).
acar alpha-carotene (in micrograms)
bcar beta-carotene (in micrograms)
cryp beta-cryptoxanthin (in micrograms)
lyco lycopene (in micrograms)
lz lutein and zeaxanthin (in micrograms).
vb1 thiamin (vitamin B1, in milligrams)
vb2 riboflavin (vitamin B2, in milligrams)
niac niacin (in milligrams)
vb6 vitamin B5 (in milligrams)
fola total folate (in micrograms)
fa folic acid (in micrograms)

ff food folate (in micrograms)
 ch1 total choline (in milligrams)
 vb12 vitamin B12 (in micrograms)
 vc vitamin C (in milligrams)
 vd vitamin D (comprising D2 and D3, in micrograms)
 vk vitamin K (in micrograms)
 calc calcium (in milligrams)
 phos phosphorus (in milligrams)
 magn magnesium (in milligrams)
 iron iron (in milligrams)
 zinc zinc (in milligrams)
 copp copper (in milligrams)
 sodi sodium (in milligrams)
 pota potassium (in milligrams)
 sele selenium (in micrograms)

Details

Note that the sample design oversampled specific population targets and that only respondents are provided. The website contains more information about sampling weights. There are multiple missing records.

Note

These data are subject to a data user agreement, available at https://www.cdc.gov/nchs/data_access/restrictions.htm

Source

National Center for Health Statistics, https://www.cdc.gov/Nchs/Nhanes/2015-2016/DR1TOT_I.XPT

pandemics

Deaths from pandemics

Description

The data base contains estimated records of the number of deaths from pandemics.

Usage

pandemics

Format

A data frame with 72 rows and 8 variables:

event name of the event
 startyear start year of the event
 endyear end year of the event
 lower lower bound on estimated deaths (in thousands)
 average average estimated deaths (in thousands)
 upper upper bound on estimated deaths (in thousands)
 saverage scaled average of estimated deaths (in thousands)
 population estimated population at risk (in thousands)

Source

Cirillo, P. and N.N. Taleb (2020). *Tail risk of contagious diseases*. Nat. Phys. **16**, 606–613 (2020).
 <doi:10.1038/s41567-020-0921-x>

 plot.eprof

Plot of (modified) profile likelihood

Description

The function plots the (modified) profile likelihood and the tangent exponential profile likelihood

Usage

```
## S3 method for class 'eprof'
plot(x, ...)
```

Arguments

x an object of class eprof returned by [gpd.pll](#) or [gev.pll](#).
 ... further arguments to plot.

Value

a graph of the (modified) profile likelihoods

References

Brazzale, A. R., Davison, A. C. and Reid, N. (2007). *Applied Asymptotics: Case Studies in Small-Sample Statistics*. Cambridge University Press, Cambridge.

Severini, T. A. (2000). *Likelihood Methods in Statistics*. Oxford University Press, Oxford.

`plot.fr`*Plot of tangent exponential model profile likelihood*

Description

This function is adapted from the `plot.fr` function from the `hoa` package bundle. It differs from the latter mostly in the placement of legends.

Usage

```
## S3 method for class 'fr'  
plot(x, ...)
```

Arguments

`x` an object of class `fr` returned by [gpd.tem](#) or [gev.tem](#).
`...` further arguments to `plot` currently ignored. Providing a numeric vector which allows for custom selection of the plots. A logical `all`. See **Details**.

Details

Plots produced depend on the integers provided in `which`. 1 displays the Wald pivot, the likelihood root r , the modified likelihood root r^* and the likelihood modification q as functions of the parameter ψ . 2 gives the renormalized profile log likelihood and adjusted form, with the maximum likelihood having ordinate value of zero. 3 provides the significance function, a transformation of 1. Lastly, 4 plots the correction factor as a function of the likelihood root; it is a diagnostic plot aimed for detecting failure of the asymptotic approximation, often due to poor numerics in a neighborhood of $r=0$; the function should be smooth. The function [spline.corr](#) is designed to handle this by correcting numerically unstable estimates, replacing outliers and missing values with the fitted values from the fit.

Value

graphs depending on argument `which`

References

Brazzale, A. R., Davison, A. C. and Reid, N. (2007). *Applied Asymptotics: Case Studies in Small-Sample Statistics*. Cambridge University Press, Cambridge.

pp *Poisson process of extremes.*

Description

Likelihood, score function and information matrix for the Poisson process likelihood.

Arguments

par	vector of loc, scale and shape
dat	sample vector
u	threshold
method	string indicating whether to use the expected ('exp') or the observed ('obs' - the default) information matrix.
np	number of periods of observations. This is a <i>post hoc</i> adjustment for the intensity so that the parameters of the model coincide with those of a generalized extreme value distribution with block size $\text{length}(\text{dat})/\text{np}$.
nobs	number of observations for the expected information matrix. Default to $\text{length}(\text{dat})$ if dat is provided.

Usage

```
pp.ll(par, dat)
pp.ll(par, dat, u, np)
pp.score(par, dat)
pp.infomat(par, dat, method = c('obs', 'exp'))
```

Functions

- `pp.ll`: log likelihood
- `pp.score`: score vector
- `pp.infomat`: observed or expected information matrix

Author(s)

Leo Belzile

References

- Coles, S. (2001). *An Introduction to Statistical Modeling of Extreme Values*, Springer, 209 p.
- Wadsworth, J.L. (2016). Exploiting Structure of Maximum Likelihood Estimators for Extreme Value Threshold Selection, *Technometrics*, **58**(1), 116-126, <http://dx.doi.org/10.1080/00401706.2014.998345>.
- Sharkey, P. and J.A. Tawn (2017). A Poisson process reparameterisation for Bayesian inference for extremes, *Extremes*, **20**(2), 239-263, <http://dx.doi.org/10.1007/s10687-016-0280-2>.

rdir	<i>Random variate generation for Dirichlet distribution on S_d</i>
------	---

Description

A function to sample Dirichlet random variables, based on the representation as ratios of Gamma. Note that the RNG will generate on the full simplex and the sum to one constraint is respected here

Usage

```
rdir(n, alpha, normalize = TRUE)
```

Arguments

n	sample size
alpha	vector of parameter
normalize	boolean. If FALSE, the function returns Gamma variates with parameter alpha.

Value

sample of dimension d (size of alpha) from the Dirichlet distribution.

Examples

```
rdir(n=100, alpha=c(0.5,0.5,2),TRUE)
rdir(n=100, alpha=c(3,1,2),FALSE)
```

rgparp	<i>Simulation from generalized R-Pareto processes</i>
--------	---

Description

The generalized R-Pareto process is supported on $(loc - scale / shape, Inf)$ if $shape > 0$, or $(-Inf, loc - scale / shape)$ for negative shape parameters, conditional on $(X - r(loc)) / r(scale) > 0$. The standard Pareto process corresponds to $scale = loc = rep(1, d)$.

Usage

```
rgparp(
  n,
  shape = 1,
  thresh = 1,
  risk = c("mean", "sum", "site", "max", "min", "l2"),
  siteindex = NULL,
  d,
```

```

loc,
scale,
param,
sigma,
model = c("log", "neglog", "bilog", "negbilog", "hr", "br", "xstud", "smith",
"schlather", "ct", "sdir", "dirmix"),
weights,
vario,
coord = NULL,
...
)

```

Arguments

n	number of observations
shape	shape parameter of the generalized Pareto variable
thresh	univariate threshold for the exceedances of risk functional
risk	string indicating the risk functional.
siteindex	integer between 1 and d specifying the index of the site or variable
d	dimension of sample
loc	location vector
scale	scale vector
param	parameter vector for the logistic, bilogistic, negative bilogistic and extremal Dirichlet (Coles and Tawn) model. Parameter matrix for the Dirichlet mixture. Degree of freedoms for extremal student model. See Details .
sigma	covariance matrix for Brown-Resnick and extremal Student-t distributions. Symmetric matrix of squared coefficients λ^2 for the Husler-Reiss model, with zero diagonal elements.
model	for multivariate extreme value distributions, users can choose between 1-parameter logistic and negative logistic, asymmetric logistic and negative logistic, bilogistic, Husler-Reiss, extremal Dirichlet model (Coles and Tawn) or the Dirichlet mixture. Spatial models include the Brown-Resnick, Smith, Schlather and extremal Student max-stable processes. Max linear models are also supported
weights	vector of length m for the m mixture components that sum to one. For the "maxlin" model, weights should be a matrix with d columns that represent the weight of the components and whose column sum to one (if provided, this argument overrides asy).
vario	semivariogram function whose first argument must be distance. Used only if provided in conjunction with coord and if sigma is missing
coord	d by k matrix of coordinates, used as input in the variogram vario or as parameter for the Smith model. If grid is TRUE, unique entries should be supplied.
...	additional arguments for the vario function

Value

an n by d sample from the generalized R-Pareto process, with attributes `accept.rate` if the procedure uses rejection sampling.

Examples

```
rgparp(n = 10, risk = 'site', siteindex = 2, d = 3, param = 2.5,
       model = 'log', scale = c(1, 2, 3), loc = c(2, 3, 4))
rgparp(n = 10, risk = 'max', d = 4, param = c(0.2, 0.1, 0.9, 0.5),
       scale = 1:4, loc = 1:4, model = 'bilog')
rgparp(n = 10, risk = 'sum', d = 3, param = c(0.8, 1.2, 0.6, -0.5),
       scale = 1:3, loc = 1:3, model = 'sdir')
vario <- function(x, scale = 0.5, alpha = 0.8){ scale*x^alpha }
grid.coord <- as.matrix(expand.grid(runif(4), runif(4)))
rgparp(n = 10, risk = 'max', vario = vario, coord = grid.coord,
       model = 'br', scale = runif(16), loc = rnorm(16))
```

 rlarg

Distribution of the r-largest observations

Description

Likelihood, score function and information matrix for the r -largest observations likelihood.

Arguments

<code>par</code>	vector of <code>loc</code> , <code>scale</code> and <code>shape</code>
<code>dat</code>	an n by r sample matrix, ordered from largest to smallest in each row
<code>method</code>	string indicating whether to use the expected ('exp') or the observed ('obs' - the default) information matrix.
<code>nobs</code>	number of observations for the expected information matrix. Default to <code>nrow(dat)</code> if <code>dat</code> is provided.
<code>r</code>	number of order statistics kept. Default to <code>ncol(dat)</code>

Usage

```
rlarg.ll(par, dat, u, np)
rlarg.score(par, dat)
rlarg.infomat(par, dat, method = c('obs', 'exp'), nobs = nrow(dat), r = ncol(dat))
```

Functions

- `rlarg.ll`: log likelihood
- `rlarg.score`: score vector
- `rlarg.infomat`: observed or expected information matrix

Author(s)

Leo Belzile

References

- Coles, S. (2001). *An Introduction to Statistical Modeling of Extreme Values*, Springer, 209 p.
- Smith, R.L. (1986). Extreme value theory based on the r largest annual events, *Journal of Hydrology*, **86**(1-2), 27–43, [http://dx.doi.org/10.1016/0022-1694\(86\)90004-1](http://dx.doi.org/10.1016/0022-1694(86)90004-1).

rmev

*Exact simulations of multivariate extreme value distributions***Description**

Implementation of the random number generators for multivariate extreme-value distributions and max-stable processes based on the two algorithms described in Dombry, Engelke and Oesting (2016).

Usage

```
rmev(
  n,
  d,
  param,
  asy,
  sigma,
  model = c("log", "alog", "neglog", "aneglog", "bilog", "negbilog", "hr", "br", "xstud",
            "smith", "schlather", "ct", "sdir", "dirmix", "pairbeta", "pairexp", "wdirbs",
            "wexpbs", "maxlin"),
  alg = c("ef", "sm"),
  weights = NULL,
  vario = NULL,
  coord = NULL,
  grid = FALSE,
  dist = NULL,
  ...
)
```

Arguments

n	number of observations
d	dimension of sample
param	parameter vector for the logistic, bilogistic, negative bilogistic and extremal Dirichlet (Coles and Tawn) model. Parameter matrix for the Dirichlet mixture. Degree of freedoms for extremal student model. See Details .

asy	list of asymmetry parameters, as in function <code>rmvevd</code> from package <code>evd</code> , of $2^d - 1$ vectors of size corresponding to the power set of d , with sum to one constraints.
sigma	covariance matrix for Brown-Resnick and extremal Student-t distributions. Symmetric matrix of squared coefficients λ^2 for the Husler-Reiss model, with zero diagonal elements.
model	for multivariate extreme value distributions, users can choose between 1-parameter logistic and negative logistic, asymmetric logistic and negative logistic, bilogistic, Husler-Reiss, extremal Dirichlet model (Coles and Tawn) or the Dirichlet mixture. Spatial models include the Brown-Resnick, Smith, Schlather and extremal Student max-stable processes. Max linear models are also supported
alg	algorithm, either simulation via extremal function ('ef') or via the spectral measure ('sm'). Default to ef.
weights	vector of length m for the m mixture components that sum to one. For the "maxlin" model, weights should be a matrix with d columns that represent the weight of the components and whose column sum to one (if provided, this argument overrides asy).
vario	semivariogram function whose first argument must be distance. Used only if provided in conjunction with <code>coord</code> and if <code>sigma</code> is missing
coord	d by k matrix of coordinates, used as input in the variogram <code>vario</code> or as parameter for the Smith model. If <code>grid</code> is TRUE, unique entries should be supplied.
grid	Logical. TRUE if the coordinates are two-dimensional grid points (spatial models).
dist	symmetric matrix of pairwise distances. Default to NULL.
...	additional arguments for the <code>vario</code> function

Details

The vector `param` differs depending on the model

- `log`: one dimensional parameter greater than 1
- `alog`: $2^d - d - 1$ dimensional parameter for dep. Values are recycled if needed.
- `neglog`: one dimensional positive parameter
- `aneglog`: $2^d - d - 1$ dimensional parameter for dep. Values are recycled if needed.
- `bilog`: d -dimensional vector of parameters in $[0, 1]$
- `negbilog`: d -dimensional vector of negative parameters
- `ct`, `dir`, `negdir`, `sdir`: d -dimensional vector of positive (a)symmetry parameters. For `dir` and `negdir`, a $d + 1$ vector consisting of the d Dirichlet parameters and the last entry is an index of regular variation in $(-\min(\alpha_1, \dots, \alpha_d), 1]$ treated as shape parameter
- `xstud`: one dimensional parameter corresponding to degrees of freedom α
- `dirmix`: d by m -dimensional matrix of positive (a)symmetry parameters
- `pairbeta`, `pairexp`: $d(d-1)/2+1$ vector of parameters, containing the concentration parameter and the coefficients of the pairwise beta, in lexicographical order e.g., $\beta_{12}, \beta_{13}, \dots$
- `wdirbs`, `wexpbs`: $2d$ vector of d concentration parameters followed by the d Dirichlet parameters

Stephenson points out that the multivariate asymmetric negative logistic model given in e.g. Coles and Tawn (1991) is not a valid distribution function in dimension $d > 3$ unless additional constraints are imposed on the parameter values. The implementation in `rmev` uses the same construction as the asymmetric logistic distribution (see the vignette). As such it does not match the bivariate implementation of `rbvevd`.

The dependence parameter of the `evd` package for the Husler-Reiss distribution can be recovered taking for the Brown–Resnick model $2/r = \sqrt{(2\gamma(h))}$ where h is the lag vector between sites and $r = 1/\lambda$ for the Husler–Reiss.

Value

an n by d exact sample from the corresponding multivariate extreme value model

Warning

As of version 1.8 (August 16, 2016), there is a distinction between models `hr` and `br`. The latter is meant to be used in conjunction with variograms. The parametrization differs between the two models.

The family of scaled Dirichlet is now parametrized by a parameter in $-\min(\alpha)$ appended to the d vector `param` containing the parameter `alpha` of the Dirichlet model. Arguments `model='dir'` and `model='negdir'` are still supported internally, but not listed in the options.

Author(s)

Leo Belzile

References

Dombry, Engelke and Oesting (2016). Exact simulation of max-stable processes, *Biometrika*, **103**(2), 303–317.

See Also

[rmevspec](#), [rmvevd](#), [rbvevd](#)

Examples

```
set.seed(1)
rmev(n=100, d=3, param=2.5, model='log', alg='ef')
rmev(n=100, d=4, param=c(0.2,0.1,0.9,0.5), model='bilog', alg='sm')
## Spatial example using power variogram
#NEW: Semi-variogram must take distance as argument
semivario <- function(x, scale, alpha){ scale*x^alpha }
#grid specification
grid.coord <- as.matrix(expand.grid(runif(4), runif(4)))
rmev(n=100, vario=semivario, coord=grid.coord, model='br', scale = 0.5, alpha = 1)
#using the Brown-Resnick model with a covariance matrix
vario2cov <- function(coord, semivario,...){
  sapply(1:nrow(coord), function(i) sapply(1:nrow(coord), function(j)
    semivario(sqrt(sum((coord[i,])^2)), ...) +
```

```

semivario(sqrt(sum((coord[j,]^2)), ...) -
semivario(sqrt(sum((coord[i,]-coord[j,]^2)), ...)))
}
rmev(n=100, sigma=vario2cov(grid.coord, semivario = semivario, scale = 0.5, alpha = 1), model='br')
# asymmetric logistic model - see function 'rmvevd' from package 'evd'
asy <- list(0, 0, 0, 0, c(0,0), c(0,0), c(0,0), c(0,0), c(0,0), c(0,0),
c(.2,.1,.2), c(.1,.1,.2), c(.3,.4,.1), c(.2,.2,.2), c(.4,.6,.2,.5))
rmev(n=1, d=4, param=0.3, asy=asy, model="alog")
#Example with a grid (generating an array)
rmev(n=10, sigma=cbind(c(2,1), c(1,3)), coord=cbind(runif(4), runif(4)), model='smith', grid=TRUE)
## Example with Dirichlet mixture
alpha.mat <- cbind(c(2,1,1),c(1,2,1),c(1,1,2))
rmev(n=100, param=alpha.mat, weights=rep(1/3,3), model='dirmix')
rmev(n=10, param=c(0.1,1,2,3), d=3, model='pairbeta')

```

rmevspec

Random samples from spectral distributions of multivariate extreme value models.

Description

Generate from Q_i , the spectral measure of a given multivariate extreme value model based on the L1 norm.

Usage

```

rmevspec(
  n,
  d,
  param,
  sigma,
  model = c("log", "neglog", "bilog", "negbilog", "hr", "br", "xstud", "smith",
"schlather", "ct", "sdir", "dirmix", "pairbeta", "pairexp", "wdirbs", "wexpbs",
"maxlin"),
  weights = NULL,
  vario = NULL,
  coord = NULL,
  grid = FALSE,
  dist = NULL,
  ...
)

```

Arguments

n number of observations

d dimension of sample

param parameter vector for the logistic, bilogistic, negative bilogistic and extremal Dirichlet (Coles and Tawn) model. Parameter matrix for the Dirichlet mixture. Degree of freedoms for extremal student model. See **Details**.

sigma	covariance matrix for Brown-Resnick and extremal Student-t distributions. Symmetric matrix of squared coefficients λ^2 for the Husler-Reiss model, with zero diagonal elements.
model	for multivariate extreme value distributions, users can choose between 1-parameter logistic and negative logistic, asymmetric logistic and negative logistic, bilogistic, Husler-Reiss, extremal Dirichlet model (Coles and Tawn) or the Dirichlet mixture. Spatial models include the Brown-Resnick, Smith, Schlather and extremal Student max-stable processes. Max linear models are also supported
weights	vector of length m for the m mixture components that sum to one. For the "maxlin" model, weights should be a matrix with d columns that represent the weight of the components and whose column sum to one (if provided, this argument overrides asy).
vario	semivariogram function whose first argument must be distance. Used only if provided in conjunction with coord and if sigma is missing
coord	d by k matrix of coordinates, used as input in the variogram vario or as parameter for the Smith model. If grid is TRUE, unique entries should be supplied.
grid	Logical. TRUE if the coordinates are two-dimensional grid points (spatial models).
dist	symmetric matrix of pairwise distances. Default to NULL.
...	additional arguments for the vario function

Details

The vector param differs depending on the model

- log: one dimensional parameter greater than 1
- neglog: one dimensional positive parameter
- bilog: d-dimensional vector of parameters in $[0, 1]$
- negbilog: d-dimensional vector of negative parameters
- ct, dir, negdir: d-dimensional vector of positive (a)symmetry parameters. Alternatively, a $d + 1$ vector consisting of the d Dirichlet parameters and the last entry is an index of regular variation in $(0, 1]$ treated as scale
- xstud: one dimensional parameter corresponding to degrees of freedom alpha
- dirmix: d by m-dimensional matrix of positive (a)symmetry parameters
- pairbeta, pairexp: $d(d-1)/2+1$ vector of parameters, containing the concentration parameter and the coefficients of the pairwise beta, in lexicographical order e.g., $\beta_{1,2}, \beta_{1,3}, \dots$
- wdirbs, wexpbs: 2d vector of d concentration parameters followed by the d Dirichlet parameters

Value

an n by d exact sample from the corresponding multivariate extreme value model

Note

This functionality can be useful to generate for example Pareto processes with marginal exceedances.

Author(s)

Leo Belzile

References

Dombry, Engelke and Oesting (2016). Exact simulation of max-stable processes, *Biometrika*, **103**(2), 303–317.

Boldi (2009). A note on the representation of parametric models for multivariate extremes. *Extremes* **12**, 211–218.

Examples

```
set.seed(1)
rmevspec(n=100, d=3, param=2.5, model='log')
rmevspec(n=100, d=3, param=2.5, model='neglog')
rmevspec(n=100, d=4, param=c(0.2,0.1,0.9,0.5), model='bilog')
rmevspec(n=100, d=2, param=c(0.8,1.2), model='ct') #Dirichlet model
rmevspec(n=100, d=2, param=c(0.8,1.2,0.5), model='sdir') #with additional scale parameter
#Variogram gamma(h) = scale*||h||^alpha
#NEW: Variogram must take distance as argument
vario <- function(x, scale=0.5, alpha=0.8){ scale*x^alpha }
#grid specification
grid.coord <- as.matrix(expand.grid(runif(4), runif(4)))
rmevspec(n=100, vario=vario, coord=grid.coord, model='br')
## Example with Dirichlet mixture
alpha.mat <- cbind(c(2,1,1),c(1,2,1),c(1,1,2))
rmevspec(n=100, param=alpha.mat, weights=rep(1/3,3), model='dirmix')
```

rparp

Simulation from R-Pareto processes

Description

Simulation from R-Pareto processes

Usage

```
rparp(
  n,
  shape = 1,
  risk = c("sum", "site", "max", "min", "l2"),
  siteindex = NULL,
  d,
  param,
  sigma,
  model = c("log", "neglog", "bilog", "negbilog", "hr", "br", "xstud", "smith",
    "schlather", "ct", "sdir", "dirmix"),
  weights,
```

```

    vario,
    coord = NULL,
    ...
)

```

Arguments

n	number of observations
shape	shape tail index of Pareto variable
risk	string indicating risk functional.
siteindex	integer between 1 and d specifying the index of the site or variable
d	dimension of sample
param	parameter vector for the logistic, bilogistic, negative bilogistic and extremal Dirichlet (Coles and Tawn) model. Parameter matrix for the Dirichlet mixture. Degree of freedoms for extremal student model. See Details .
sigma	covariance matrix for Brown-Resnick and extremal Student-t distributions. Symmetric matrix of squared coefficients λ^2 for the Husler-Reiss model, with zero diagonal elements.
model	for multivariate extreme value distributions, users can choose between 1-parameter logistic and negative logistic, asymmetric logistic and negative logistic, bilogistic, Husler-Reiss, extremal Dirichlet model (Coles and Tawn) or the Dirichlet mixture. Spatial models include the Brown-Resnick, Smith, Schlather and extremal Student max-stable processes. Max linear models are also supported
weights	vector of length m for the m mixture components that sum to one. For the "maxlin" model, weights should be a matrix with d columns that represent the weight of the components and whose column sum to one (if provided, this argument overrides asy).
vario	semivariogram function whose first argument must be distance. Used only if provided in conjunction with coord and if sigma is missing
coord	d by k matrix of coordinates, used as input in the variogram vario or as parameter for the Smith model. If grid is TRUE, unique entries should be supplied.
...	additional arguments for the vario function

Details

For riskf=max and riskf=min, the procedure uses rejection sampling based on Pareto variates sampled from sum and may be slow if d is large.

Value

an n by d sample from the R-Pareto process, with attributes accept.rate if the procedure uses rejection sampling.

Examples

```
rparp(n=10, risk = 'site', siteindex=2, d=3, param=2.5, model='log')
rparp(n=10, risk = 'min', d=3, param=2.5, model='neglog')
rparp(n=10, risk = 'max', d=4, param=c(0.2,0.1,0.9,0.5), model='bilog')
rparp(n=10, risk = 'sum', d=3, param=c(0.8,1.2,0.6, -0.5), model='sdir')
vario <- function(x, scale=0.5, alpha=0.8){ scale*x^alpha }
grid.coord <- as.matrix(expand.grid(runif(4), runif(4)))
rparp(n=10, risk = 'max', vario=vario, coord=grid.coord, model='br')
```

rparpcs

Simulation from Pareto processes using composition sampling

Description

The algorithm performs forward sampling by simulating first from a mixture, then sample angles conditional on them being less than (max) or greater than (min) one. The resulting sample from the angular distribution is then multiplied by Pareto variates with tail index shape.

Usage

```
rparpcs(
  n,
  model = c("log", "neglog", "br", "xstud"),
  risk = c("max", "min"),
  param = NULL,
  d,
  Lambda = NULL,
  Sigma = NULL,
  df = NULL,
  shape = 1,
  ...
)
```

Arguments

n	sample size.
model	string indicating the model family.
risk	string indicating the risk functional. Only max and min are currently supported.
param	parameter value for the logistic or negative logistic model
d	dimension of the multivariate model, only needed for logistic or negative logistic models
Lambda	parameter matrix for the Brown–Resnick model. See Details .
Sigma	correlation matrix if model = 'xstud', otherwise the covariance matrix formed from the stationary Brown-Resnick process.
df	degrees of freedom for extremal Student process.

shape tail index of the Pareto variates (reciprocal shape parameter). Must be strictly positive.
 ... additional parameters, currently ignored

Details

For the moment, only exchangeable models and models based n elliptical processes are handled. The parametrization of the Brown–Resnick is in terms of the matrix Lambda, which is formed by evaluating the semivariogram γ at sites s_i, s_j , meaning that $\Lambda_{i,j} = \gamma(s_i, s_j)/2$. The argument Sigma is ignored for the Brown-Resnick model if Lambda is provided by the user.

Value

an n by d matrix of samples, where $d = \text{ncol}(\text{Sigma})$, with attributes `mixt.weights`.

Author(s)

Leo Belzile

See Also

[rparp](#) for general simulation of Pareto processes based on an accept-reject algorithm.

Examples

```
## Not run:
#Brown-Resnick, Wadsworth and Tawn (2014) parametrization
D <- 20L
coord <- cbind(runif(D), runif(D))
semivario <- function(d, alpha = 1.5, lambda = 1){0.5 * (d/lambda)^alpha}
Lambda <- semivario(as.matrix(dist(coord))) / 2
rparpcs(n = 10, Lambda = Lambda, model = 'br', shape = 0.1)
#Extremal Student
Sigma <- stats::rWishart(n = 1, df = 20, Sigma = diag(10))[, , 1]
rparpcs(n = 10, Sigma = cov2cor(Sigma), df = 3, model = 'xstud')

## End(Not run)
```

rparpcshr

Simulation of generalized Huesler-Reiss Pareto vectors via composition sampling

Description

Sample from the generalized Pareto process associated to Huesler-Reiss spectral profiles. For the Huesler-Reiss Pareto vectors, the matrix Sigma is utilized to build Q viz.

$$Q = \Sigma^{-1} - \frac{\Sigma^{-1} \mathbf{1}_d \mathbf{1}_d^\top \Sigma^{-1}}{\mathbf{1}_d^\top \Sigma^{-1} \mathbf{1}_d}.$$

The location vector m and Sigma are the parameters of the underlying log-Gaussian process.

Usage

```
rparpcshr(n, u, alpha, Sigma, m)
```

Arguments

n	sample size
u	vector of marginal location parameters (must be strictly positive)
alpha	vector of shape parameters (must be strictly positive).
Sigma	covariance matrix of process, used to define Q . See Details .
m	location vector of Gaussian distribution.

Value

n by d matrix of observations

References

Ho, Z. W. O and C. Dombry (2019), Simple models for multivariate regular variations and the Huesler-Reiss Pareto distribution, *Journal of Multivariate Analysis* (**173**), p. 525-550, [doi:10.1016/j.jmva.2019.04.008](https://doi.org/10.1016/j.jmva.2019.04.008)

Examples

```
D <- 20L
coord <- cbind(runif(D), runif(D))
di <- as.matrix(dist(rbind(c(0, ncol(coord)), coord)))
semivario <- function(d, alpha = 1.5, lambda = 1){(d/lambda)^alpha}
Vmat <- semivario(di)
Sigma <- outer(Vmat[-1, 1], Vmat[1, -1], '+') - Vmat[-1, -1]
m <- Vmat[-1,1]
## Not run:
samp <- rparpcshr(n = 100, u = c(rep(1, 10), rep(2, 10)),
  alpha = seq(0.1, 1, length = 20), Sigma = Sigma, m = m)
## End(Not run)
```

 rrlarg

Simulate r-largest observations from point process of extremes

Description

Simulate the r-largest observations from a Poisson point process with intensity

$$\Lambda(x) = (1 + \xi(x - \mu)/\sigma)^{-1/\xi}$$

Usage

```
rrlarg(n, r, loc = 0, scale = 1, shape = 0)
```

Arguments

n	sample size
r	number of observations per block
loc	location parameter
scale	scale parameter
shape	shape parameter

Value

an n by r matrix of samples from the point process, ordered from largest to smallest in each row.

scoreindep

Ramos and Ledford test of independence

Description

The Ramos and Ledford (2005) score test of independence is a modification of tests by Tawn (1988) and Ledford and Tawn (1996) for a logistic model parameter $\alpha = 1$; the latter two have scores with zero expectation, but the variance of the score are infinite, which produces non-regularity and yield test, once suitably normalized, that converge slowly to their asymptotic null distribution. The test, designed for bivariate samples, transforms observations to have unit Frechet margins and considers a bivariate censored likelihood approach for the logistic distribution.

Usage

```
scoreindep(xdat, p, test = c("ledford", "tawn"))
```

Arguments

xdat	a n by 2 matrix of observations
p	probability level for the marginal threshold
test	string; if tawn, only censor observations in the upper quadrant when both variables are large as in Tawn (1988), otherwise censor marginally for ledford as in Ledford and Tawn (1996).

Value

	a list with elements
stat	value of the score test statistic
pval	asymptotic p-value
test	test argument

Examples

```
samp <- rmev(n = 1000, d = 2,  
  param = 0.99, model = "log")  
scoreindep(samp, p = 0.9)
```

shape.genquant

Beirlant et al. generalized quantile shape estimator

Description

This estimator estimates the real shape parameter based on generalized quantile plots based on mean excess functions, generalized median excesses or trimmed mean excesses.

Usage

```
shape.genquant(  
  xdat,  
  k,  
  type = c("genmean", "genmed", "trimmean"),  
  weight,  
  p = 0.5  
)
```

Arguments

xdat n vector of observations

k number of upper order statistics

type string indicating the estimator choice, one of genmean, genmed and trimmean.

weight weight a kernel function on $[0, 1]$

References

Beirlant, J., Vynckier P. and J.L. Teugels (1996). *Excess functions and estimation of the extreme-value index*. Bernoulli, 2(4), 293-318.

shape.hill	<i>Hill's estimator of the shape parameter</i>
------------	--

Description

Given a sample of positive observations, calculate the tail index or shape parameter. The shape estimate returned is positive.

Usage

```
shape.hill(xdat, k)
```

Arguments

xdat	vector of positive observations
kmin	minimum number of upper order statistics (exceedances) for the estimator
kmax	maximum number of upper order statistics (exceedances) for the estimator

Value

a data frame with the number of order statistics k and the shape parameter estimate `shape`, or a single numeric value if `kmin` equals `kmax`.

References

Hill, B.M. (1975). *A simple general approach to inference about the tail of a distribution*. *Annals of Statistics*, **3**, 1163-1173.

Examples

```
xdat <- mev::rgp(n = 200, loc = 1, scale = 0.5, shape = 0.5)
shape.hill(xdat)
```

shape.moment	<i>Dekkers and de Haan moment estimator for the shape</i>
--------------	---

Description

Given a sample of exceedances, compute the moment estimator of the real shape parameter.

Usage

```
shape.moment(xdat, k)
```

Arguments

xdat vector of positive observations of length n
k number of largest order statistics

Value

a data frame with the number of order statistics k and the shape parameter estimate `shape`, or a single numeric value if k is a scalar.

References

Dekkers, A.L.M. and de Haan, L. (1989). *On the estimation of the extreme-value index and large quantile estimation.*, Annals of Statistics, **17**, 1795-1833.

shape.pickands	<i>Pickand's shape estimator</i>
----------------	----------------------------------

Description

Given a sample of size n of positive exceedances, compute the real shape parameter ξ based on the k largest order statistics.

Usage

```
shape.pickands(xdat, k)
```

Arguments

xdat vector of positive observations of length n
k number of largest order statistics

Value

a data frame with the number of order statistics k and the shape parameter estimate `shape`, or a single numeric value if k is a scalar.

References

Pickands, III, J. (1975). *Statistical inference using extreme order statistics.* Annals of Statistics, **3**, 119-131.

shape.pickandsxu	<i>Extreme U-statistic Pickands estimator</i>
------------------	---

Description

Given a random sample of n exceedances, the estimator returns an estimator of the shape parameter or extreme value index using a kernel of order 3, based on k largest exceedances of x_{dat} . Oorschot et al. (2023) parametrize the model in terms of $m = n - k$, so that $m = n$ corresponds to using only the three largest observations.

Usage

```
shape.pickandsxu(xdat, k, ...)
```

Arguments

xdat	vector of observations of length n
k	number of largest order statistics $3 \leq k \leq n$.

Details

The calculations are based on the recursions provided in Lemma 4.3 of Oorschot et al.

References

Oorschot, J, J. Segers and C. Zhou (2023), Tail inference using extreme U-statistics, Electron. J. Statist. 17(1): 1113-1159. [doi:10.1214/23EJS2129](https://doi.org/10.1214/23EJS2129)

Examples

```
xdat <- rgp(n = 1000, shape = 0.2)
shape.pickandsxu(xdat, k = 10)
```

smith.penult	<i>Smith's penultimate approximations</i>
--------------	---

Description

The function takes as arguments the distribution and density functions. There are two options: `method='bm'` yields block maxima and `method='pot'` threshold exceedances. For `method='bm'`, the user should provide in such case the block sizes via the argument `m`, whereas if `method='pot'`, a vector of threshold values should be provided. The other argument (`u` or `m` depending on the method) is ignored.

Usage

```
smith.penult(family, method = c("bm", "pot"), u, qu, m, returnList = TRUE, ...)
```

Arguments

family	the name of the parametric family. Will be used to obtain dfamily, pfamily, qfamily
method	either block maxima ('bm') or peaks-over-threshold ('pot') are supported
u	vector of thresholds for method 'pot'
qu	vector of quantiles for method 'pot'. Ignored if argument u is provided.
m	vector of block sizes for method 'bm'
returnList	logical; should the arguments be returned as a list or as a matrix of parameter
...	additional arguments passed to densF and distF

Details

Alternatively, the user can provide functions densF, quantF and distF for the density, quantile function and distribution functions, respectively. The user can also supply the derivative of the density function, ddensF. If the latter is missing, it will be approximated using finite-differences.

For method = "pot", the function computes the reciprocal hazard and its derivative on the log scale to avoid numerical overflow. Thus, the density function should have argument log and the distribution function arguments log.p and lower.tail, respectively.

Value

either a vector, a matrix if either length(m)>1 or length(u)>1 or a list (if returnList) containing

- loc: location parameters (method='bm')
- scale: scale parameters
- shape: shape parameters
- u: thresholds (if method='pot'), percentile corresponding to threshold (if method='pot')
- m: block sizes (if method='bm')

Author(s)

Leo Belzile

References

Smith, R.L. (1987). Approximations in extreme value theory. *Technical report 205*, Center for Stochastic Process, University of North Carolina, 1–34.

Examples

```
#Threshold exceedance for Normal variables
qu <- seq(1,5,by=0.02)
penult <- smith.penult(family = "norm", ddensF=function(x){-x*dnorm(x)},
  method = 'pot', u = qu)
plot(qu, penult$shape, type='l', xlab='Quantile',
  ylab='Penultimate shape', ylim=c(-0.5,0))
#Block maxima for Gamma variables -
```



```

#User must provide arguments for shape (or rate)
m <- seq(30, 3650, by=30)
penult <- smith.penult(family = 'gamma', method = 'bm', m=m, shape=0.1)
plot(m, penult$shape, type='l', xlab='Quantile', ylab='Penultimate shape')

#Comparing density of GEV approximation with true density of maxima
m <- 100 #block of size 100
p <- smith.penult(family='norm',
  ddensF=function(x){-x*dnorm(x)}, method='bm', m=m, returnList=FALSE)
x <- seq(1, 5, by = 0.01)
plot(x, m*dnorm(x)*exp((m-1)*pnorm(x,log.p=TRUE)),type='l', ylab='Density',
  main='Distribution of the maxima of\n 100 standard normal variates')
lines(x, mev::dgev(x,loc=p[1], scale=p[2], shape=0),col=2)
lines(x, mev::dgev(x,loc=p[1], scale=p[2], shape=p[3]),col=3)
legend(x = 'topright',lty = c(1,1,1,1), col = c(1,2,3,4),
  legend = c('exact', 'ultimate', 'penultimate'), bty = 'n')

```

spunif

Semi-parametric marginal transformation to uniform

Description

The function spunif transforms a matrix or vector of data x to the pseudo-uniform scale using a semiparametric transform. Data below the threshold are transformed to pseudo-uniforms using a rank transform, while data above the threshold are assumed to follow a generalized Pareto distribution. The parameters of the latter are estimated using maximum likelihood if either `scale = NULL` or `shape = NULL`.

Usage

```
spunif(x, thresh, scale = NULL, shape = NULL)
```

Arguments

<code>x</code>	matrix or vector of data
<code>thresh</code>	vector of marginal thresholds
<code>scale</code>	vector of marginal scale parameters for the generalized Pareto
<code>shape</code>	vector of marginal shape parameters for the generalized Pareto

Value

a matrix or vector of the same dimension as x , with pseudo-uniform observations

Author(s)

Leo Belzile

Examples

```
x <- rmev(1000, d = 3, param = 2, model = 'log')
thresh <- apply(x, 2, quantile, 0.95)
spunif(x, thresh)
```

taildep

Coefficient of tail correlation and tail dependence

Description

For data with unit Pareto margins, the coefficient of tail dependence η is defined via

$$\Pr(\min(X) > x) = L(x)x^{-1/\eta},$$

where $L(x)$ is a slowly varying function. Ignoring the latter, several estimators of η can be defined. In unit Pareto margins, η is a nonnegative shape parameter that can be estimated by fitting a generalized Pareto distribution above a high threshold. In exponential margins, η is a scale parameter and the maximum likelihood estimator of the latter is the Hill estimator. Both methods are based on peaks-over-threshold and the user can choose between pointwise confidence confint obtained through a likelihood ratio test statistic ("lrt") or the Wald statistic ("wald").

Usage

```
taildep(
  data,
  u = NULL,
  nq = 40,
  qlim = c(0.8, 0.99),
  depmeas = c("eta", "chi"),
  method = list(eta = c("emp", "betacop", "gpd", "hill"), chi = c("emp", "betacop")),
  confint = c("wald", "lrt"),
  level = 0.95,
  trunc = TRUE,
  empirical.transformation = TRUE,
  ties.method = "random",
  plot = TRUE,
  ...
)
```

Arguments

data	an n by d matrix of multivariate observations
u	vector of percentiles between 0 and 1
nq	number of quantiles of the structural variable at which to form a grid; only used if u = NULL.
qlim	limits for the sequence u of the structural variable

depmeas	dependence measure, either of "eta" or "chi"
method	named list giving the estimation method for eta and chi. Default to "emp" for both.
confint	string indicating the type of confidence interval for η , one of "wald" or "lrt"
level	the confidence level required (default to 0.95).
trunc	logical indicating whether the estimates and confidence intervals should be truncated in $[0, 1]$
empirical.transformation	logical indicating whether observations should be transformed to pseudo-uniform scale (default to TRUE); otherwise, they are assumed to be uniform
ties.method	string indicating the type of method for rank; see rank for a list of options. Default to "random"
plot	logical; should graphs be plotted?
...	additional arguments passed to plot; current support for main, xlab, ylab, add and further pch, lty, type, col for points; additional arguments for confidence intervals are handled via cipch, cilty, citype, cicol.

Details

The most common approach for estimation is the empirical survival copula, by evaluating the proportion of sample minima with uniform margins that exceed a given x . An alternative estimator uses a smoothed estimator of the survival copula using Bernstein polynomial, resulting in the so-called betacop estimator. Approximate pointwise confidence confint for the latter are obtained by assuming the proportion of points is binomial.

The coefficient of tail correlation χ is

$$\chi = \lim_{u \rightarrow 1} \frac{\Pr(F_1(X_1) > u, \dots, F_D(X_D) > u)}{1 - u}.$$

Asymptotically independent vectors have $\chi = 0$. The estimator uses an estimator of the survival copula

Value

a named list with elements

- u: a K vector of percentile levels
- eta: a K by 3 matrix with point estimates, lower and upper confidence intervals
- chi: a K by 3 matrix with point estimates, lower and upper confidence intervals

Note

As of version 1.15, the percentiles used are from the minimum variable. This ensures that, regardless of the number of variables, there is no error message returned because the quantile levels are too low for there to be observations

See Also

[chplot](#) for bivariate empirical estimates of χ and $\bar{\chi}$.

Examples

```
## Not run:
set.seed(765)
# Max-stable model
dat <- rmev(n = 1000, d = 4, param = 0.7, model = "log")
taildep(dat, confint = 'wald')

## End(Not run)
```

tstab.gpd

Parameter stability plots for peaks-over-threshold

Description

This function computes the maximum likelihood estimate at each provided threshold and plots the estimates (pointwise), along with 95 or else from 1000 independent draws from the posterior distribution under vague independent normal prior on the log-scale and shape. The latter two methods better reflect the asymmetry of the estimates than the Wald confidence intervals.

Usage

```
tstab.gpd(
  xdat,
  thresh,
  method = c("wald", "profile", "post"),
  level = 0.95,
  plot = TRUE,
  which = c("scale", "shape"),
  changepar = TRUE,
  ...
)
```

Arguments

xdat	a vector of observations
thresh	a vector of candidate thresholds at which to compute the estimates.
method	string indicating the method for computing confidence or credible intervals. Must be one of "wald", "profile" or "post".
level	confidence level of the intervals. Default to 0.95.
plot	logical; should parameter stability plots be displayed? Default to TRUE.
which	character vector with elements scale or shape
changepar	logical; if TRUE, changes the graphical parameters.
...	additional arguments passed to plot.

Value

a list with components

- `threshold`: vector of numerical threshold values.
- `mle`: matrix of modified scale and shape maximum likelihood estimates.
- `lower`: matrix of lower bounds for the confidence or credible intervals.
- `upper`: matrix of lower bounds for the confidence or credible intervals.
- `method`: method for the confidence or coverage intervals.

plots of the modified scale and shape parameters, with pointwise confidence/credible intervals and an invisible data frame containing the threshold `thresh` and the modified scale and shape parameters.

Note

The function is hard coded to prevent fitting a generalized Pareto distribution to samples of size less than 10. If the estimated shape parameters are all on the boundary of the parameter space (meaning $\hat{\xi} = -1$), then the plots return one-sided confidence intervals for both the modified scale and shape parameters: these typically suggest that the chosen thresholds are too high for estimation to be reliable.

Author(s)

Leo Belzile

See Also

[gpd.fitrange](#)

Examples

```
dat <- abs(rnorm(10000))
u <- qnorm(seq(0.9,0.99, by= 0.01))
par(mfrow = c(1,2))
tstab.gpd(xdat = dat, thresh = u, changepar = FALSE)
## Not run:
tstab.gpd(xdat = dat, thresh = u, method = "profile")
tstab.gpd(xdat = dat, thresh = u, method = "post")

## End(Not run)
```

venice

Venice Sea Levels

Description

The venice data contains the 10 largest yearly sea levels (in cm) from 1887 until 2019. Only the yearly maximum is available for 1922 and the six largest observations for 1936.

Format

a data frame with 133 rows and 11 columns containing the year of the measurement (first column) and ordered 10-largest yearly observations, reported in decreasing order from largest (r_1) to smallest (r_{10}).

Note

Smith (1986) notes that the annual maxima seems to fluctuate around a constant sea level up to 1930 or so, after which there is potential linear trend. Records of threshold exceedances above 80 cm (reported on the website) indicate that observations are temporally clustered.

The observations from 1931 until 1981 can be found in Table 1 in Smith (1986), who reported data from Pirazzoli (1982). The values from 1983 until 2019 were extracted by Anthony Davison from the City of Venice website (accessed in May 2020) and are licensed under the CC BY-NC-SA 3.0 license. The Venice City website indicates that later measurements were recorded by an instrument located in Punta Salute.

Source

City of Venice, Historical archive <<https://www.comune.venezia.it/node/6214>>. Last accessed November 5th, 2020.

References

Smith, R. L. (1986) Extreme value theory based on the r largest annual events. *Journal of Hydrology* **86**, 27–43.

Pirazzoli, P., 1982. Maree estreme a Venezia (periodo 1872-1981). *Acqua Aria* **10**, 1023-1039.

Coles, S. G. (2001) *An Introduction to Statistical Modelling of Extreme Values*. London: Springer.

See Also

[venice](#)

vmetric.diag	<i>Metric-based threshold selection</i>
--------------	---

Description

Adaptation of Varty et al.'s metric-based threshold automated diagnostic for the independent and identically distributed case with no rounding.

Usage

```
vmetric.diag(
  xdat,
  thresh,
  B = 199L,
  type = c("qq", "pp"),
  dist = c("l1", "l2"),
  neval = 1000L,
  ci = 0.95
)
```

Arguments

xdat	vector of observations
thresh	vector of thresholds
B	number of bootstrap replications
type	string indicating scale, either qq for exponential quantile-quantile plot or pp for probability-probability plot (uniform)
dist	string indicating norm, either l1 for absolute error or l2 for quadratic error
neval	number of points at which to estimate the metric. Default to 1000L
ci	level of symmetric confidence interval. Default to 0.95

Details

The algorithm proceeds by first computing the maximum likelihood algorithm and then simulating datasets from replication with parameters drawn from a bivariate normal approximation to the maximum likelihood estimator distribution.

For each bootstrap sample, we refit the model and convert the quantiles to exponential or uniform variates. The mean absolute or mean squared distance is calculated on these. The threshold returned is the one with the lowest value of the metric.

Value

an invisible list with components

- thresh: scalar threshold minimizing criterion

- cthresh: vector of candidate thresholds
- metric: value of the metric criterion evaluated at each threshold
- type: argument type
- dist: argument dist

References

Varty, Z. and J.A. Tawn and P.M. Atkinson and S. Bierman (2021+), Inference for extreme earthquake magnitudes accounting for a time-varying measurement process

W.diag	<i>Wadsworth's univariate and bivariate exponential threshold diagnostics</i>
--------	---

Description

Function to produce diagnostic plots and test statistics for the threshold diagnostics exploiting structure of maximum likelihood estimators based on the non-homogeneous Poisson process likelihood

Usage

```
W.diag(
  xdat,
  model = c("nhpp", "exp", "invexp"),
  u = NULL,
  k,
  q1 = 0,
  q2 = 1,
  par = NULL,
  M = NULL,
  nbs = 1000,
  alpha = 0.05,
  plots = c("LRT", "WN", "PS"),
  UseQuantiles = FALSE,
  changepar = TRUE,
  ...
)
```

Arguments

xdat	a numeric vector of data to be fitted.
model	string specifying whether the univariate or bivariate diagnostic should be used. Either nhpp for the univariate model, exp (invexp) for the bivariate exponential model with rate (inverse rate) parametrization. See details.
u	optional; vector of candidate thresholds.
k	number of thresholds to consider (if u unspecified).

q1	lowest quantile for the threshold sequence.
q2	upper quantile limit for the threshold sequence (q2 itself is not used as a threshold, but rather the uppermost threshold will be at the $(q_2 - 1/k) : q_2 - 1/k$ quantile).
par	parameters of the NHPP likelihood. If missing, the <code>fit.pp</code> routine will be run to obtain values
M	number of superpositions or 'blocks' / 'years' the process corresponds to (can affect the optimization)
nbs	number of simulations used to assess the null distribution of the LRT, and produce the p-value
alpha	significance level of the LRT
plots	vector of strings indicating which plots to produce; LRT= likelihood ratio test, WN = white noise, PS = parameter stability. Use NULL if you do not want plots to be produced
UseQuantiles	logical; use quantiles as the thresholds in the plot?
changeapar	logical; if TRUE, the graphical parameters (via a call to par) are modified.
...	additional parameters passed to plot, overriding defaults including

Details

The function is a wrapper for the univariate (non-homogeneous Poisson process model) and bivariate exponential dependence model. For the latter, the user can select either the rate or inverse rate parameter (the inverse rate parametrization works better for uniformity of the p-value distribution under the LR test).

There are two options for the bivariate diagnostic: either provide pairwise minimum of marginally exponentially distributed margins or provide a n times 2 matrix with the original data, which is transformed to exponential margins using the empirical distribution function.

Value

plots of the requested diagnostics and an invisible list with components

- MLE: maximum likelihood estimates from all thresholds
- Cov: joint asymptotic covariance matrix for ξ , η or $1/\eta$.
- WN: values of the white noise process
- LRT: values of the likelihood ratio test statistic vs threshold
- pval: P -value of the likelihood ratio test
- k: final number of thresholds used
- thresh: threshold selected by the likelihood ratio procedure
- qthresh: quantile level of threshold selected by the likelihood ratio procedure
- cthresh: vector of candidate thresholds
- qcthresh: quantile level of candidate thresholds
- mle.u: maximum likelihood estimates for the selected threshold
- model: model fitted

Author(s)

Jennifer L. Wadsworth

References

Wadsworth, J.L. (2016). Exploiting Structure of Maximum Likelihood Estimators for Extreme Value Threshold Selection, *Technometrics*, **58**(1), 116-126, <http://dx.doi.org/10.1080/00401706.2014.998345>.

Examples

```
## Not run:
set.seed(123)
# Parameter stability only
W.diag(xdat = abs(rnorm(5000)), model = 'nhpp',
       k = 30, q1 = 0, plots = "PS")
W.diag(rexp(1000), model = 'nhpp', k = 20, q1 = 0)
xbvn <- mvrnorm(n = 6000,
               mu = rep(0, 2),
               Sigma = cbind(c(1, 0.7), c(0.7, 1)))
# Transform margins to exponential manually
xbvn.exp <- -log(1 - pnorm(xbvn))
#rate parametrization
W.diag(xdat = apply(xbvn.exp, 1, min), model = 'exp',
       k = 30, q1 = 0)
W.diag(xdat = xbvn, model = 'exp', k = 30, q1 = 0)
#inverse rate parametrization
W.diag(xdat = apply(xbvn.exp, 1, min), model = 'invexp',
       k = 30, q1 = 0)

## End(Not run)
```

w1500m*Best 200 times of Women 1500m Track*

Description

200 all-time best performance (in seconds) of women 1500-meter run.

Format

a vector of size 200

Source

<http://www.alltime-athletics.com/w_1500ok.htm>, accessed 14.08.2018

xasym	<i>Coefficient of extremal asymmetry</i>
-------	--

Description

This function implements estimators of the bivariate coefficient of extremal asymmetry proposed in Semadeni's (2021) PhD thesis. Two estimators are implemented: one based on empirical distributions, the second using empirical likelihood.

Usage

```
xasym(
  data,
  u = NULL,
  nq = 40,
  qlim = c(0.8, 0.99),
  method = c("empirical", "emplik"),
  confint = c("none", "wald", "bootstrap"),
  level = 0.95,
  B = 999L,
  ties.method = "random",
  plot = TRUE,
  ...
)
```

Arguments

<code>data</code>	an n by 2 matrix of observations
<code>u</code>	vector of probability levels at which to evaluate extremal asymmetry
<code>nq</code>	integer; number of quantiles at which to evaluate the coefficient if <code>u</code> is NULL
<code>qlim</code>	a vector of length 2 with the probability limits for the quantiles
<code>method</code>	string indicating the estimation method, one of <code>empirical</code> or empirical likelihood (<code>emplik</code>)
<code>confint</code>	string for the method used to derive confidence intervals, either <code>none</code> (default) or a nonparametric bootstrap
<code>level</code>	probability level for confidence intervals, default to 0.95 or bounds for the interval
<code>B</code>	integer; number of bootstrap replicates (if applicable)
<code>ties.method</code>	string; method for handling ties. See the documentation of rank for available options.
<code>plot</code>	logical; if TRUE, return a plot.
<code>...</code>	additional parameters for plots

Details

Let U, V be uniform random variables and define the partial extremal dependence coefficients $\varphi_+(u) = \Pr(V > U|U > u, V > u)$, $\varphi_-(u) = \Pr(V < U|U > u, V > u)$ and $\varphi_0(u) = \Pr(V = U|U > u, V > u)$ Define

$$\varphi(u) = \frac{\varphi_+ - \varphi_-}{\varphi_+ + \varphi_-}$$

The empirical likelihood estimator, derived for max-stable vectors with unit Frechet margins, is

$$\frac{\sum_i p_i I(w_i \leq 0.5) - 0.5}{0.5 - 2 \sum_i p_i (0.5 - w_i) I(w_i \leq 0.5)}$$

where p_i is the empirical likelihood weight for observation i and w_i is the pseudo-angle associated to the first coordinate.

Value

an invisible data frame with columns

threshold vector of thresholds on the probability scale

coef extremal asymmetry coefficient estimates

confint either NULL or a matrix with two columns containing the lower and upper bounds for each threshold

References

Semadeni, C. (2020). Inference on the Angular Distribution of Extremes, PhD thesis, EPFL, no. 8168.

Examples

```
## Not run:
samp <- rmev(n = 1000,
            d = 2,
            param = 0.2,
            model = "log")
xasym(samp, confint = "wald")
xasym(samp, method = "emplik")

## End(Not run)
```

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